



# Proces zajištění a oceňování zajistných produktů v v praxi

Prosinec 2014

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# Agenda

- **Section 1** – Reinsurance Insider
- **Section 2** – Reinsurance Treaty
- **Section 3** – Proportional Reinsurance
- **Section 4** – Not Proportional Reinsurance
- **Section 5** – Pricing
- **Section 6** – Experience Rating/Burning Costs
- **Section 7** – Exposure Rating
- **Section 8** – Frequency Severity Rating
- **Section 8** – Market Comparison
- **Section 9** – Reinsurance Structures and New Trends
- **Section 10** – Reinsurance Structure Optimization

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# Reinsurance Insider

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# What is reinsurance....

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## Simply Clever

- Insurance of Insurance companies

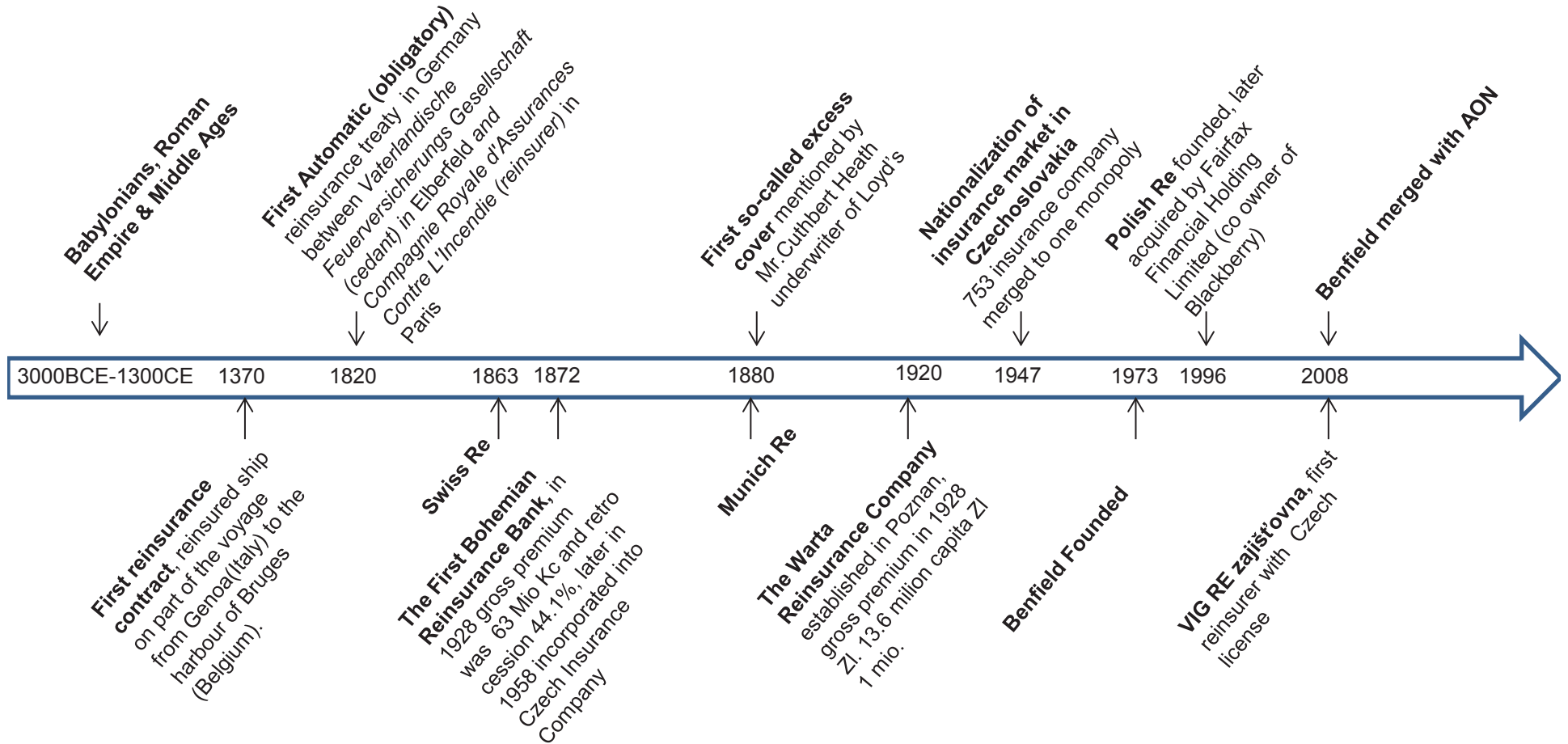
## Old School

- ***“RE-ASSURANCE, as understood by the law of England, may be said to be a contract, which the first insurer enters into, in order to relieve himself from those risks which he has incautiously undertaken, by throwing them upon other underwriters, who are called re-assurers”***
- Author: Sir James Allan Park in book *A System of the Law of Marine insurances; with three chapters on bottomry; on insurances on lives; and on insurances against fire.* 1799

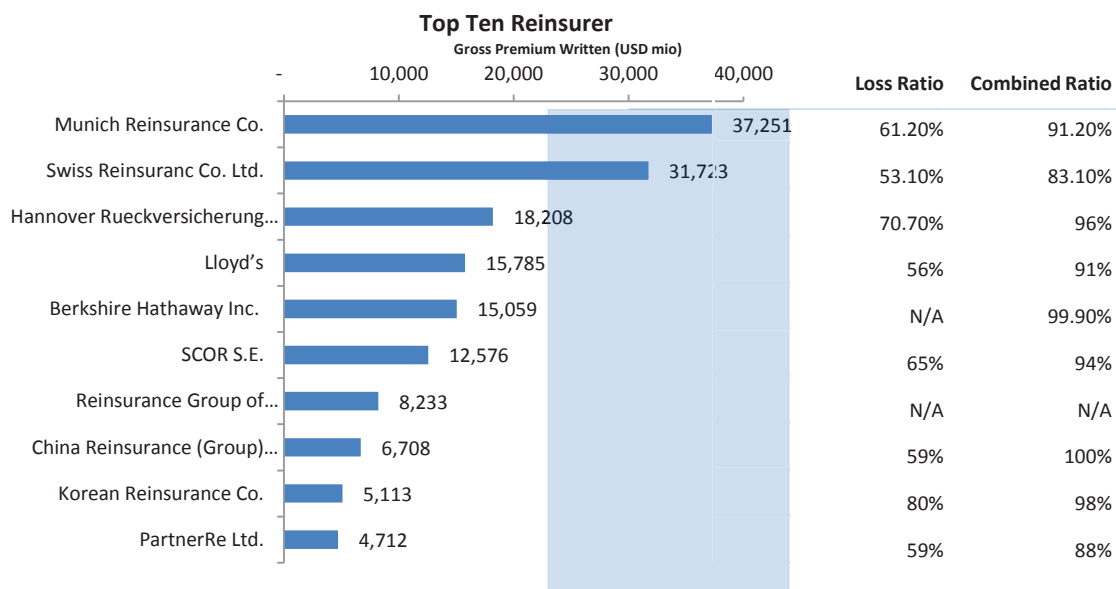
## Trendy

- ***“Reinsurance is one of the most important risk management tools used by insurers. An insurer can use reinsurance to reduce its insurance risks and the volatility of its financial results, stabilize its solvency, use its available capital more efficiently, improve its ability to withstand disasters, increase its underwriting capacity and draw on the reinsurer’s expertise with respect to product development. “***
- Source: REINSURANCE RISK MANAGEMENT GUIDELINE, Autorité des marchés financiers July 2013, Canadian Regulatory Entity

# Before...



# Reinsurance Market Concentration

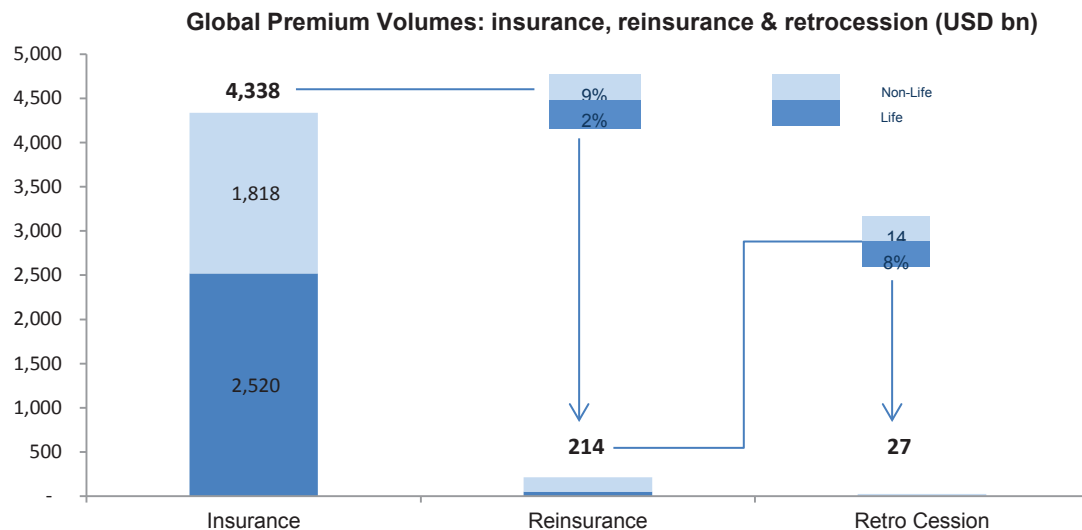


Market share of top ten reinsurers  
in **non-life**: 50.6%  
**life** : 90%

More than 200 reinsurance  
companies worldwide, 1 in Czech  
Republic, 1 in Poland

The group insurance companies of  
Berkshire Hathaway and Munich  
Re, are in top ten insurance  
ranking, 7<sup>th</sup> and 1<sup>st</sup> in terms of  
revenues

92%\* of reinsurance premium is  
ceded to reinsurers based in  
Bermuda, France, Germany,  
Ireland, Japan, UK and US.



Source: Mapfre

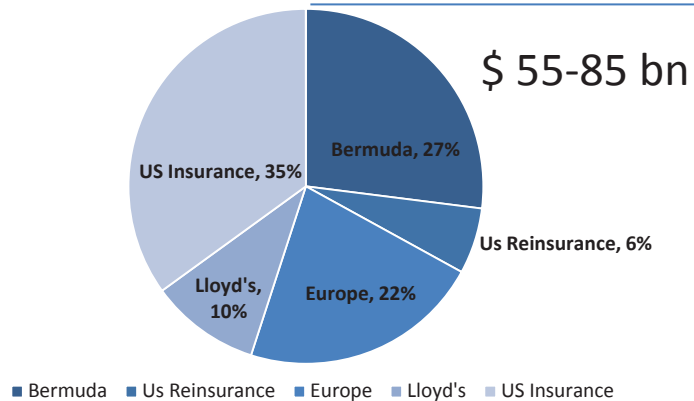
**Reinsurance Brokers** market is  
driven by three main players  
**AON Benfield**  
**Willis**  
**Marsh & McLennan**

75%\* of market share.



# Reinsurance Market is Global

US Gulf 2005 Hurricanes Losses Payments: Katrina, Wilma and Rita



Reinsurance market contributes to global risk diversification and efficient geographical capital allocation

## Hurricane Gilbert, 1988

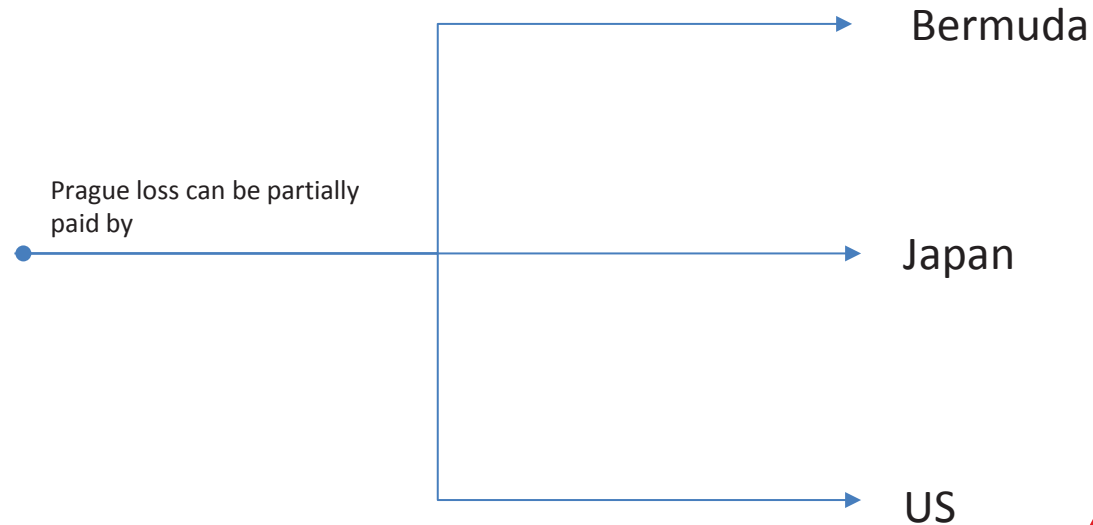
destroyed Jamaica, losses \$ 1 bn, 70% insured, only \$10 million paid by Jamaican insurance industry

Prague 2013



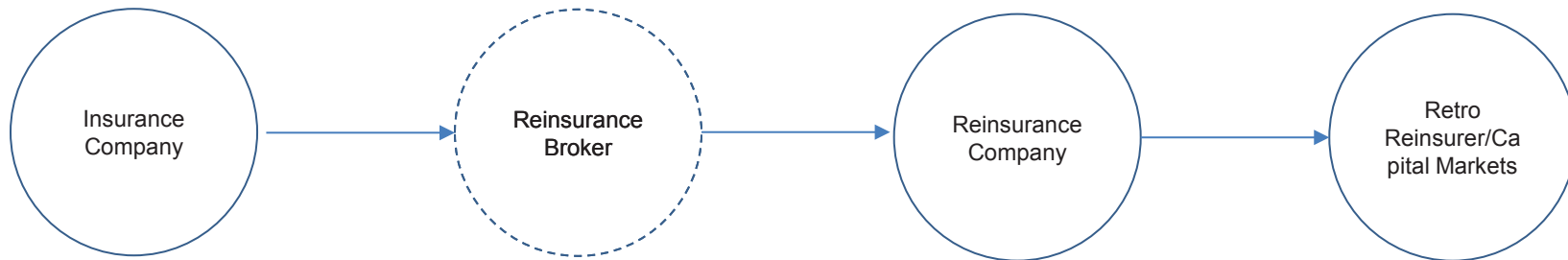
Prague 2013 Flood, Kafka Museum, Kampa

Prague loss can be partially paid by



# Reinsurance Market Participants

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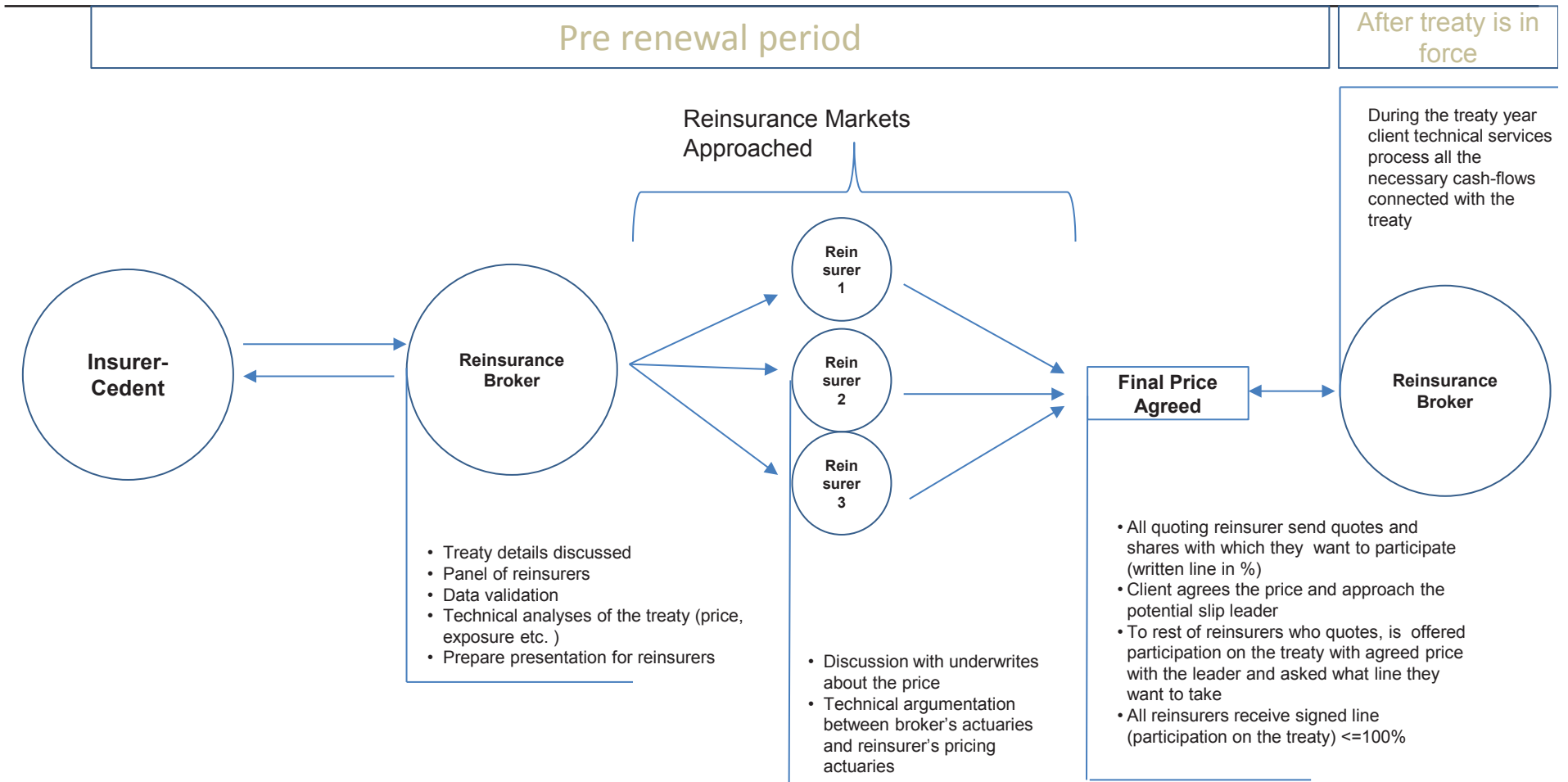


**Main function is assessment of cedent risk, structuring, placement and administration of reinsurance treaty**

1. **Brokers** negotiate/discuss with client (insurer) and reinsurers, the structure, conditions and the price of the reinsurance treaty- **stand as an opposition to reinsurers during the price negotiation**
2. **Actuaries** analyse, price and optimize reinsurance treaty, work on stochastic models for reinsurance program optimizations, spot market trends etc.
3. **Cat management** run catastrophic models (in-house models or third vendor models) on clients' portfolios, test new models and their versions, made first estimate of cat losses on client portfolio just after the cat event
4. **Model development team ( for Aon Benfield it is Impact Forecasting Team)**, works on development of catastrophic models
5. **Client technical management team**, administration of treaties (premium allocation, collection of recoveries etc.)

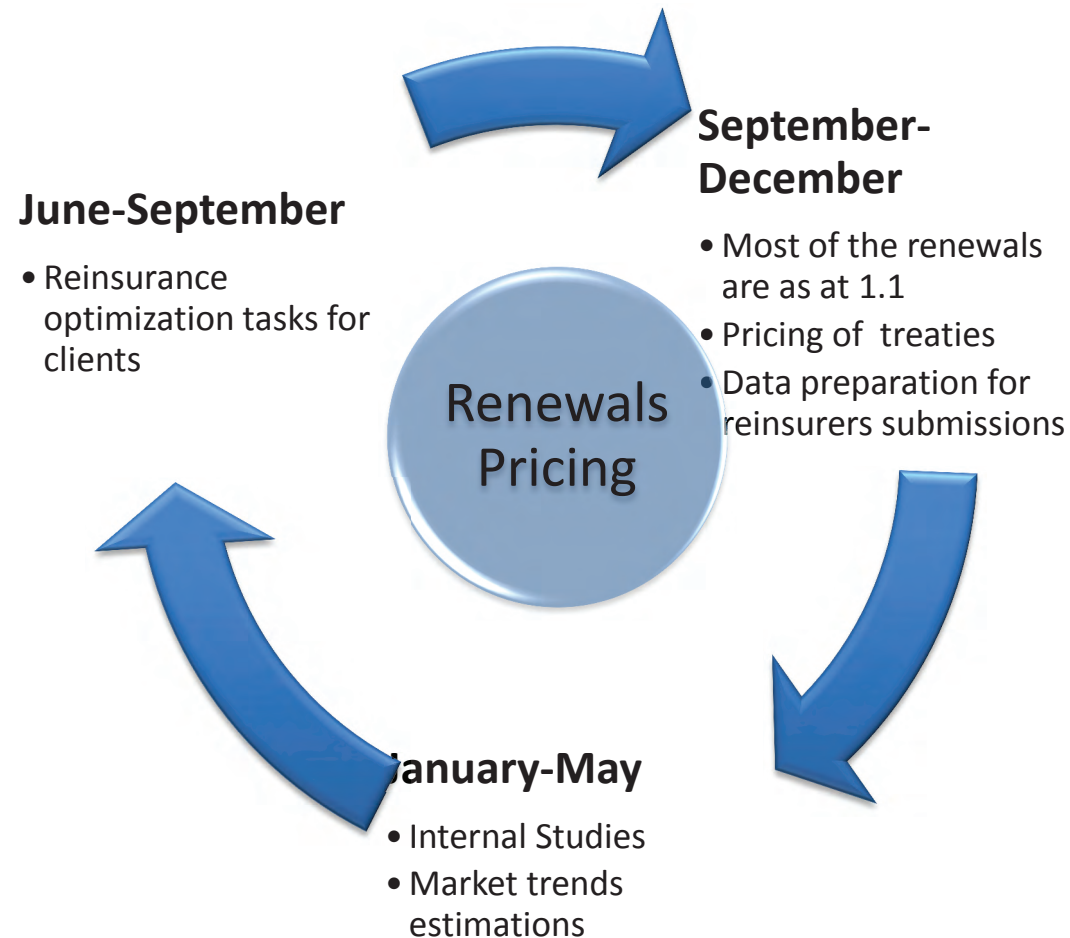


# Renewal Process of the Reinsurance Treaty



# Role of an Actuary

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# Informational Asymmetries on Reinsurance Market

## Broker's Advantage

### ➤ Experience

-Brokers place hundreds of reinsurance treaties with the most of the reinsurers in the world

### ➤ Global Overview

-broker can see prices on the market and market trends

### ➤ Technical Support

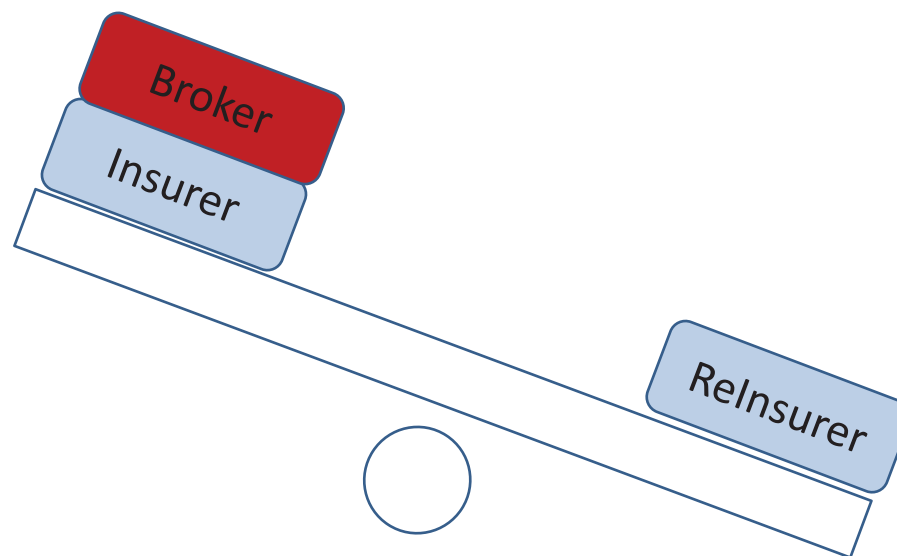
-dedicated actuaries to pricing  
-knowledge about new products, markets etc.

### ➤ Negotiation

-broker's business model is to provide cheaper reinsurance despite of fee paid by reinsurer

### ➤ High Performance

-reinsurance broker is exposed to competition



## Reinsurer's Advantage

Information advantage is on reinsurer's side, in case of direct negotiation

### ➤ No Space for Negotiation

-reinsurance manager in the insurance company can only see his/her reinsurance treaty and its conditions and price

### ➤ Lack of Benchmark

-there are no such a portal as [levnezajisteny.cz](http://levnezajisteny.cz) where you can compare your rates

### ➤ Lack of Dedicated Technical Support for Insurer

-reinsurer has devoted actuaries for pricing of incoming business



## Reinsurance Treaty

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# Classification of Reinsurance

## Obligatory (automatic) Reinsurance

- **Insurer and the reinsurer are obliged to cede and accept the risk, respectively, once conditions are agreed**
- Each risk underwritten by insurer is automatically covered by the reinsurance treaty
- **Advantages (+)**
  - Do not have to seek reinsurance per each new risk
  - Standard dates of inception and termination of the reinsurance treaty, do not have to coincide with original risks (loss occurring and risk attaching concept)
  - Higher commission than in facultative
- **Disadvantages (-)**
  - Precise definition and description of risks covered, before the inception of the treaty
  - Need to understand to exclusions of the treaty
  - Capacity of the cover is given for the whole treaty year

## Facultative Reinsurance

- **Insurer and the reinsurer have the “faculty” or option to cede or accept the risk**
- Facultative reinsurance is usually applied on risks in isolation, named and detailed individually
- **Advantages (+)**
  - Possibility to increase the underwriting capacity above the obligatory reinsurance
  - Allows underwrite risks excluded from obligatory treaty
  - Can reduce the price of automatic treaty
  - Access to reinsurer’s know-how on specific types or risk
- **Disadvantages (-)**
  - Dependence on reinsurer’s decision to underwrite or not
  - Lack of agility since it is individual and complex transaction
  - Lower commission from reinsurer than in automatic treaty, due the short term relation

Facultative-obligatory treaty is the hybrid where insurer has the possibility to cede a risk and reinsurer has an obligation to accept the risk

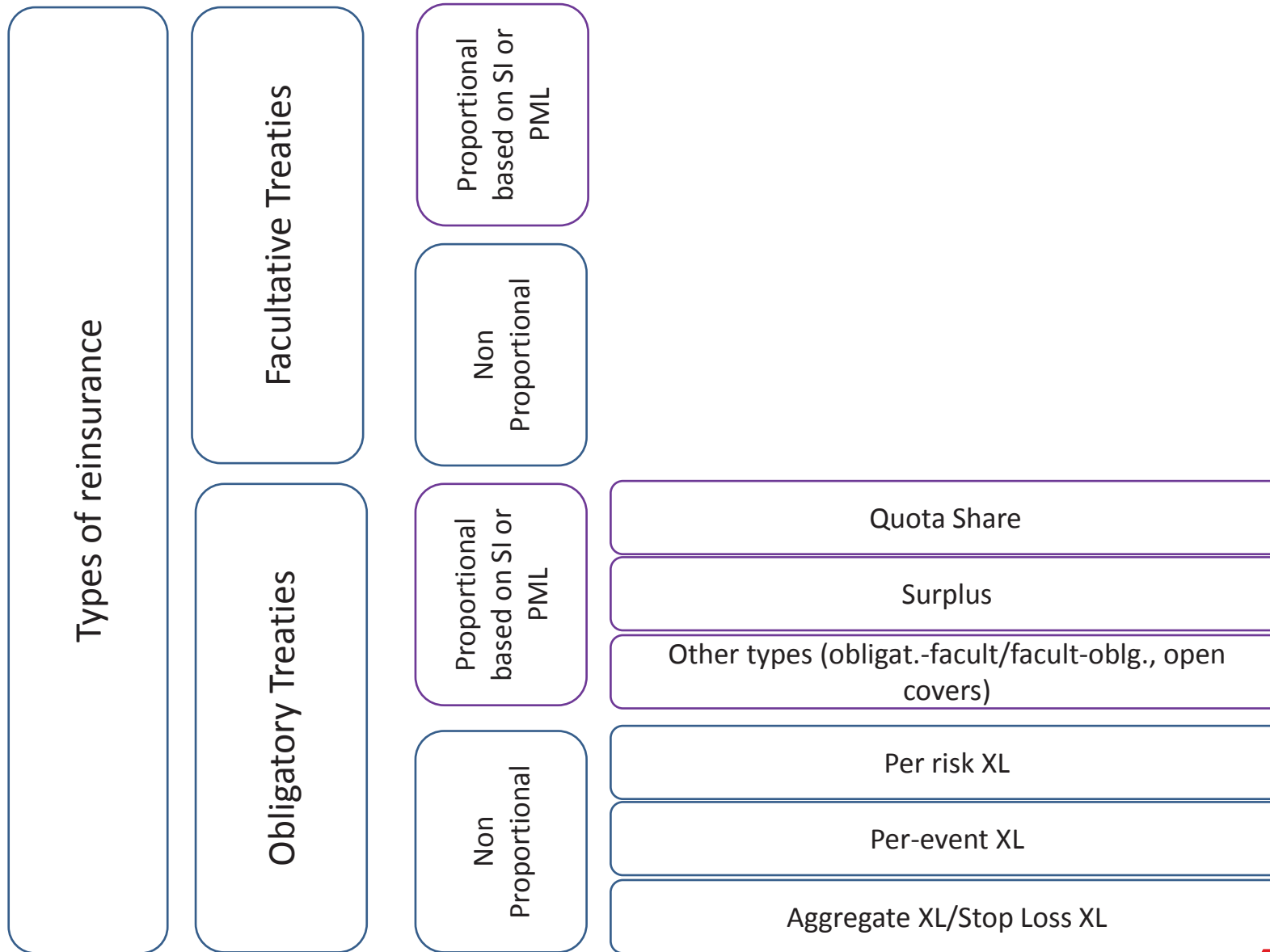
# Decision between Obligatory and Facultative Reinsurance

Risk Profile[EUR]		Number of Risk	Average PML	Premium	
PML Bands					
From	To				
0	500,000	33,115	174,009	19,840,536	Obligatory reinsurance with capacity up to EUR 172 mio
500,001	1,000,000	7,157	716,716	9,412,636	
1,000,001	2,000,000	5,258	1,378,240	9,737,979	
2,000,001	3,000,000	2,318	2,411,307	6,026,499	
3,000,001	4,000,000	1,327	3,425,731	3,838,770	
4,000,001	5,000,000	915	4,445,339	3,263,997	
5,000,001	7,500,000	1,269	6,023,954	5,210,542	
7,500,001	10,000,000	724	8,755,842	3,757,048	
10,000,001	15,000,000	530	11,987,695	3,029,078	
15,000,001	20,000,000	213	17,280,938	1,442,475	
20,000,001	30,000,000	293	25,207,972	1,734,577	Alternative obligatory reinsurance with capacity up to EUR 88 mio
30,000,001	40,000,000	108	33,758,063	812,326	
40,000,001	50,000,000	15	44,019,305	659,454	
50,000,001	80,000,000	10	62,125,636	1,394,822	
80,000,001	100,000,000	2	88,788,568	664,500	
100,000,001	125,000,000	3	111,557,792	695,844	+ Facultative cover of 4 risks
125,000,001	Higher	1	172,409,284	1,389,326	
					=

Price estimation of such solution consists from technical analyses of the treaty and crucial is the view of broker, if such a solution is "pleaceable" on the market.

- The decision to cover some risks by the facultative treaty, instead of obligatory treaty, can lead to decrease of the price of obligatory cover.

# Classification of Reinsurance







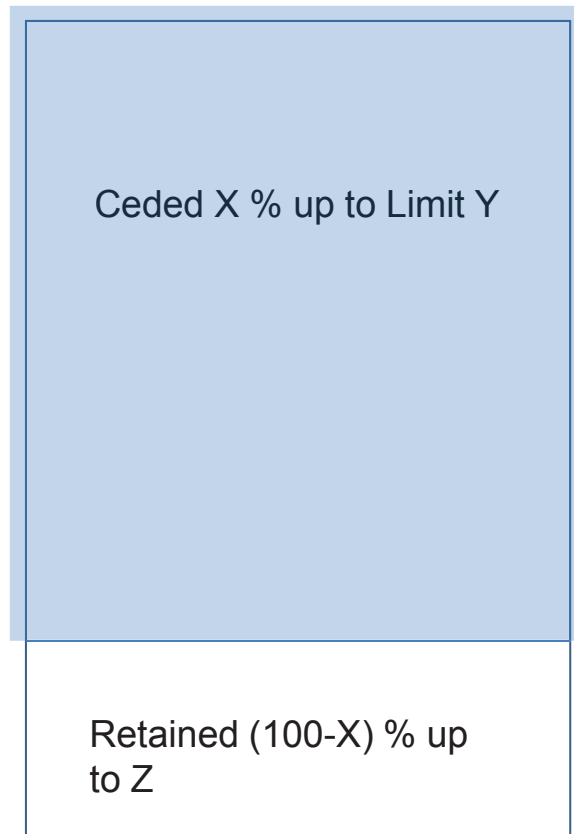
## Proportional Reinsurance

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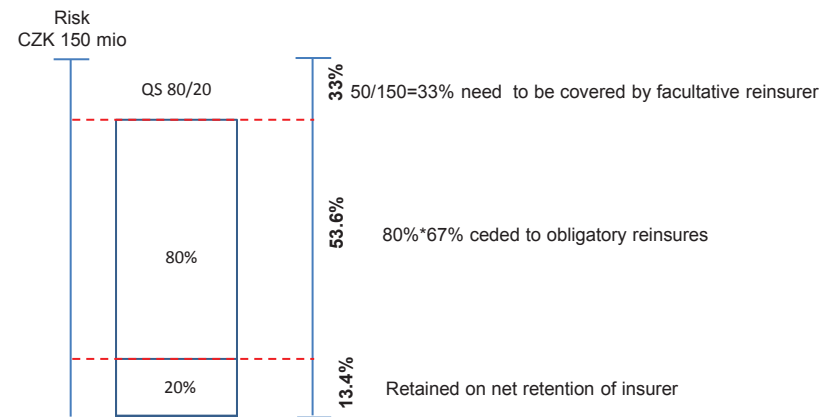
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# Quota Share

Premium and claims are ceded in the same ratio to reinsurer



- Absolute limit for quota share is agreed, reinsurer cap potential liability from accepted risk
- Example: **Quota Share 80%, capacity CZK 100 mio,**
  - Maximum retention of insurer CZK 20 mio and maximum ceded amount per claim is CZK 80 mio.
  - All claims and premium on risks below CZK 100 mio is split 20 to 80.
  - Claim on the risk above the capacity is split as follows:



- In case QS covers losses from natural perils event limit is set up in the treaty, reinsurer's liability from one nat cat event is capped at this amount

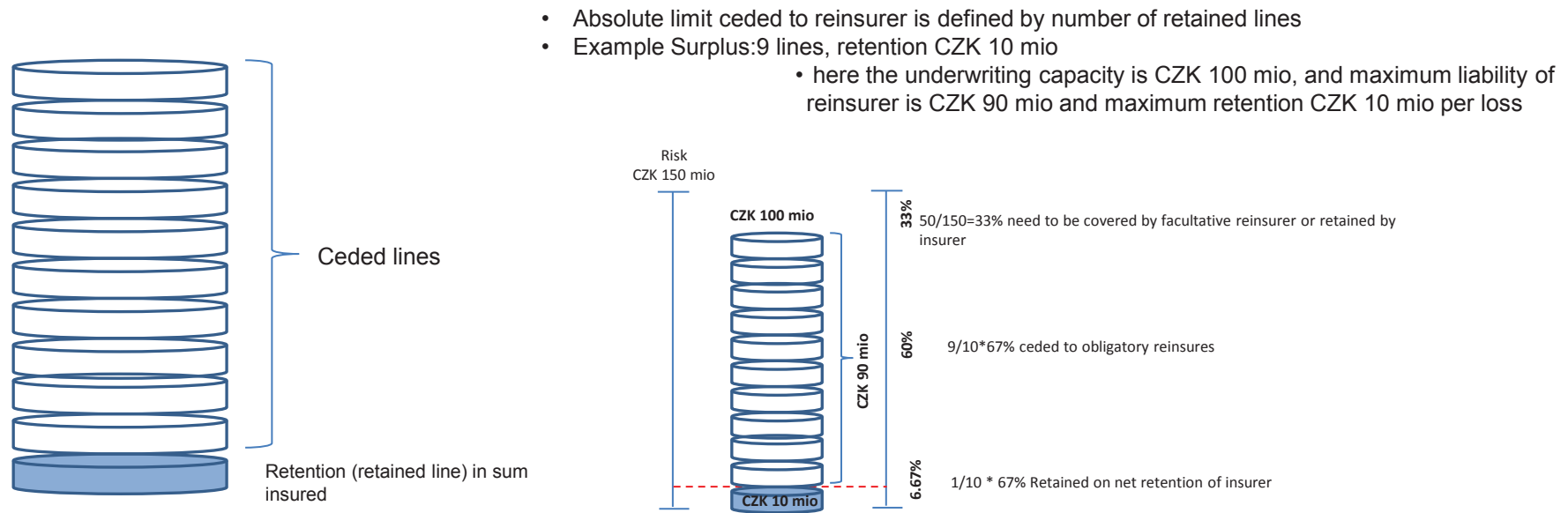
- Term limit maximum liability from the treaty for reinsurer

- (+) increase the risk capacity (insurer currently offer up to CZK 100 mio, after 50% QS can increase to CZK 200 mio net retention is still CZK 100 mio)
- (+) administrative simplicity
- (-) insurer can potentially cede profitable business to reinsurer
- (-) loss ratio remains the same, QS can not change non-profitable year to profitable, only decreases the magnitude of losses on net retention of insurer

17 Quota share is mostly used by new companies and companies that start new line of business.

# Surplus

The insurer cedes to reinsurer share of the sum insured exceeding its own retention. It is proportional treaty because premium and claims are ceded by the same percentage, on per risk basis.



- Term limit and event limit can be set up, in the same manner as for QS
- For each single risk the proportion for cession needs to be calculated
- Reinsurer can participate on small losses that happen on big risks

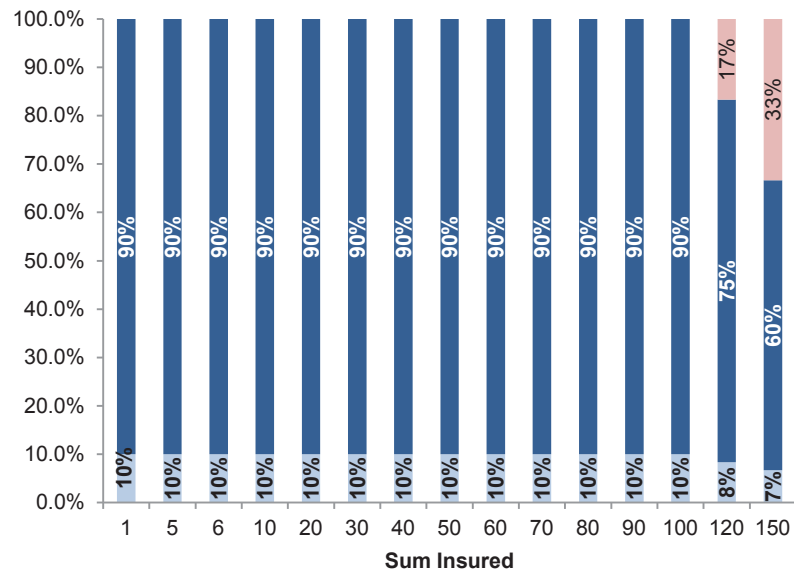
- (+) company can control on which risk does not require involvement of reinsurer
- (+) insurer retains more homogenous portfolio
- (-) administratively expensive

# Cessions to Quota Share and Surplus

## Quota Share

Cession:90%

Limit: 100

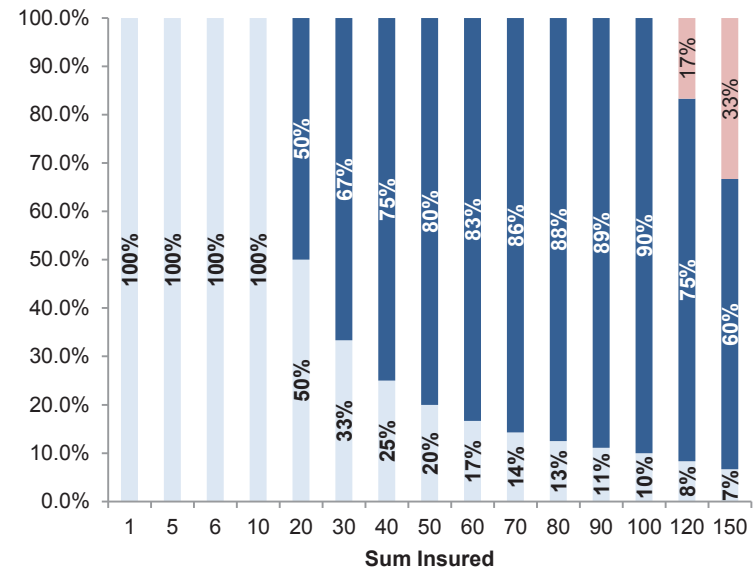


Facultative Reinsurance Ceded to Reinsurer Insurer

## Surplus

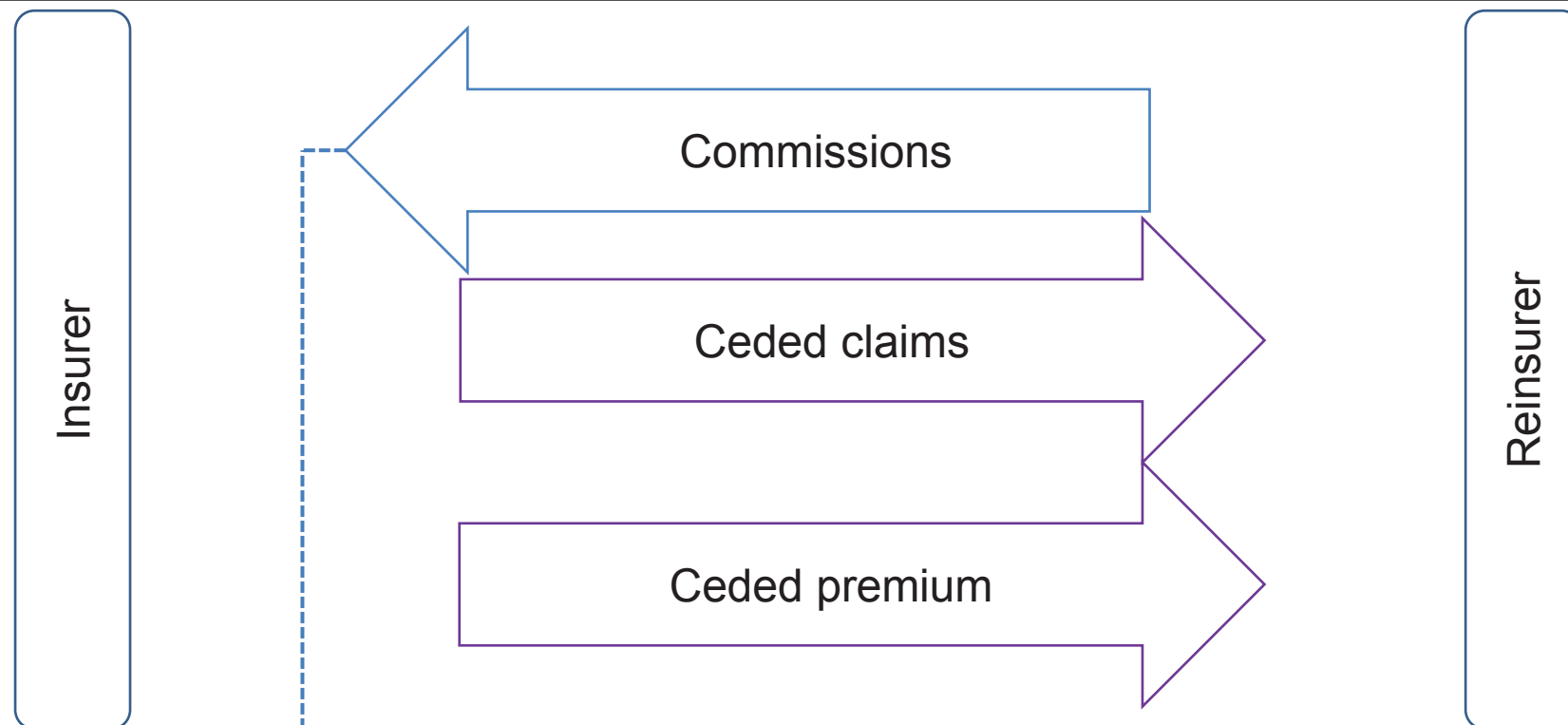
Cession:9 lines

Retention:10



Facultative Reinsurance Ceded to Reinsurer Insurer

# Cash Flow of Proportional Treaties



- a) Share on the acquisition cost of insurer
- b) Profit sharing commission from the treaty

Price of the proportional treaty is determined by the amount of commission paid back to insurer; **higher the commission, lower the price**

Insurer settles the overall balance with its reinsurer(s) once every quarter.

In case of underwriting year basis insurer needs to settle the balance with all previous reinsurer where there are some outstanding transactions for previous underwriting years, especially for losses.

In case of clean cut accounting or portfolio transfer, all outstanding liabilities with unearned premium are transferred, as at expiration of the current reinsurance treaty, to reinsurer of the following reinsurance treaty. So insurer needs to handle only one account.

# Commissions Systems for Proportional Treaties

**Fixed Commission:** flat percentage from ceded premium

- Example: 30% commission rate, premium ceded CZK 100 mio, commission CZK 30 mio
- (+) ceding company can budget its income
- (-) does not reward insurer for good results of the treaty, from reinsurer's point of view

• **Sliding-scale commission:** penalizes or rewards insurer on the base of the portfolio quality. Commission is decreased or increased based on the final loss ratio of the reinsurance treaty. Consists of defining the minimum and maximum commission for loss ratio scale.

- Provisional commission: it is fixed at the beginning of the contract and is charged to reinsurer in the periodic reinsurance account, and adjusted at a later stage within the definition of sliding scale
- Commission can never be less or more than is defined in the contract

## Example

Commission:

Minimum loss ratio 55% with commission 35%

Maximum loss ratio 70% with commission 27%

Provisional commission: 31%

Premium ceded: 100

Losses incurred: 60

Commission received

$$\text{Commission minimum} + (\text{LR}_{\text{max}} - \text{LR}_{\text{actual}}) * \frac{(\text{Com}_{\text{max}} - \text{Com}_{\text{min}})}{(\text{LR}_{\text{max}} - \text{LR}_{\text{min}})} = 32\%$$

Sliding-scale commission table

Loss Ratio		Commission
From	To	% rate
0%	55%	35%
55%	56%	34.50%
56%	57%	34.00%
57%	58%	33.50%
58%	59%	33.00%
59%	60%	32.50%
60%	61%	32.00%
61%	62%	31.50%
62%	63%	31.00%
63%	64%	30.50%
64%	65%	30.00%
65%	66%	29.50%
66%	67%	29.00%
67%	68%	28.50%
68%	69%	28.00%
69%	70%	27.50%
70%	Higher	27.00%

# Commissions Systems for Proportional Treaties

- **Profit commission:** it is very often used in the combination with fixed commission. It allows to share the profit that arises from reinsurance treaty with the cedent. Agreed percentage of the treaty profit is paid back to insurer.
- Management expenses are considered as a cost for reinsurer, this expenses can include fees to broker, cost of retro cession etc. (5%-10%).
- Loss accumulation is when loss of the treaty is carried forward for the calculation of the treaty profit, loss can be carried forward for limited period of time or until their complete extinction.
- Profit commission can be based on one reinsurance treaty but as well on more of them (e.g. different surpluses for diff. class of business so pc is calculated on combined basis)

$\text{profit commission \%} \times \max(\text{premium ceded} - \text{losses ceded} - \text{commission} - \text{management expenses} - \text{carry forward loss of the treaty}, 0)$

	Year 1	Year 2	Year 3
Premium Ceded	100	100	100
Paid Losses	90	60	60
Commision 20%	20	20	20
Reinsurer expenses 5%	5	5	5
Profit commision	20%	20%	20%
Losses carry forward	0	-15	0
Result of profit commision acc.	-15	0	15
Profit commision	0	0	3
<b>Result fo the reinsurance treaty (reinsurer point of view)</b>	<b>(10)</b>	<b>20</b>	<b>17</b>

(100-90-20-5)



# Commissions Systems for Proportional Treaties

**Loss corridor** : ceding company will reassume a portion of the reinsurer's liability if the loss ratio exceeds a certain amount. It is included in the treaty, mainly in the case of adverse results of the treaty before.

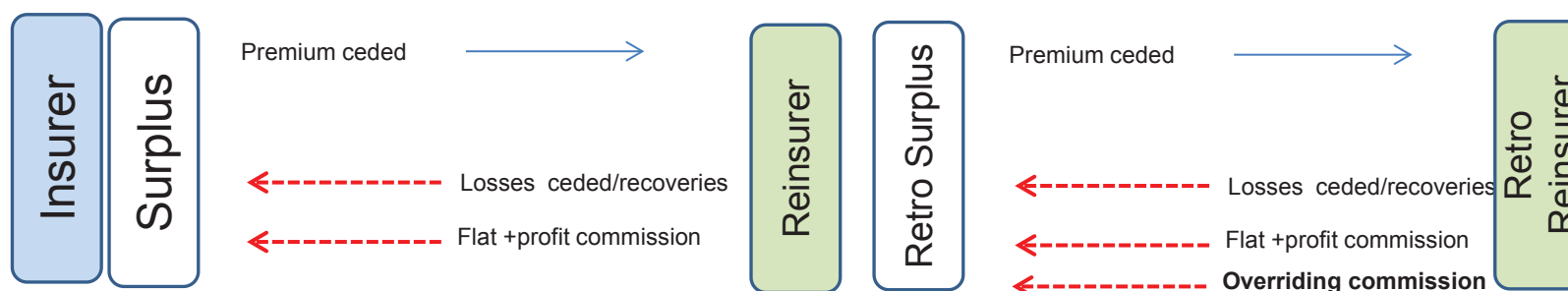
**Example:** Insurer participates by 75% of the layer from 80% to 100% loss ratio, if the reinsurer's loss ratio is 120% or higher

	Before Corridor	After Corridor
Below corridor	80%	80%
Within corridor	20%	5.0%
Above corridor	20%	20%
Total Loss Ratio	120%	105.00%

(25% of 20%)

It is a penalization of an insurer by the participation on the losses from which reinsurer can suffer.

**Overriding Commission** is a fee or percentage of money which is paid to a party responsible (retro ceding the risks) for placing a retrocession of reinsurance.





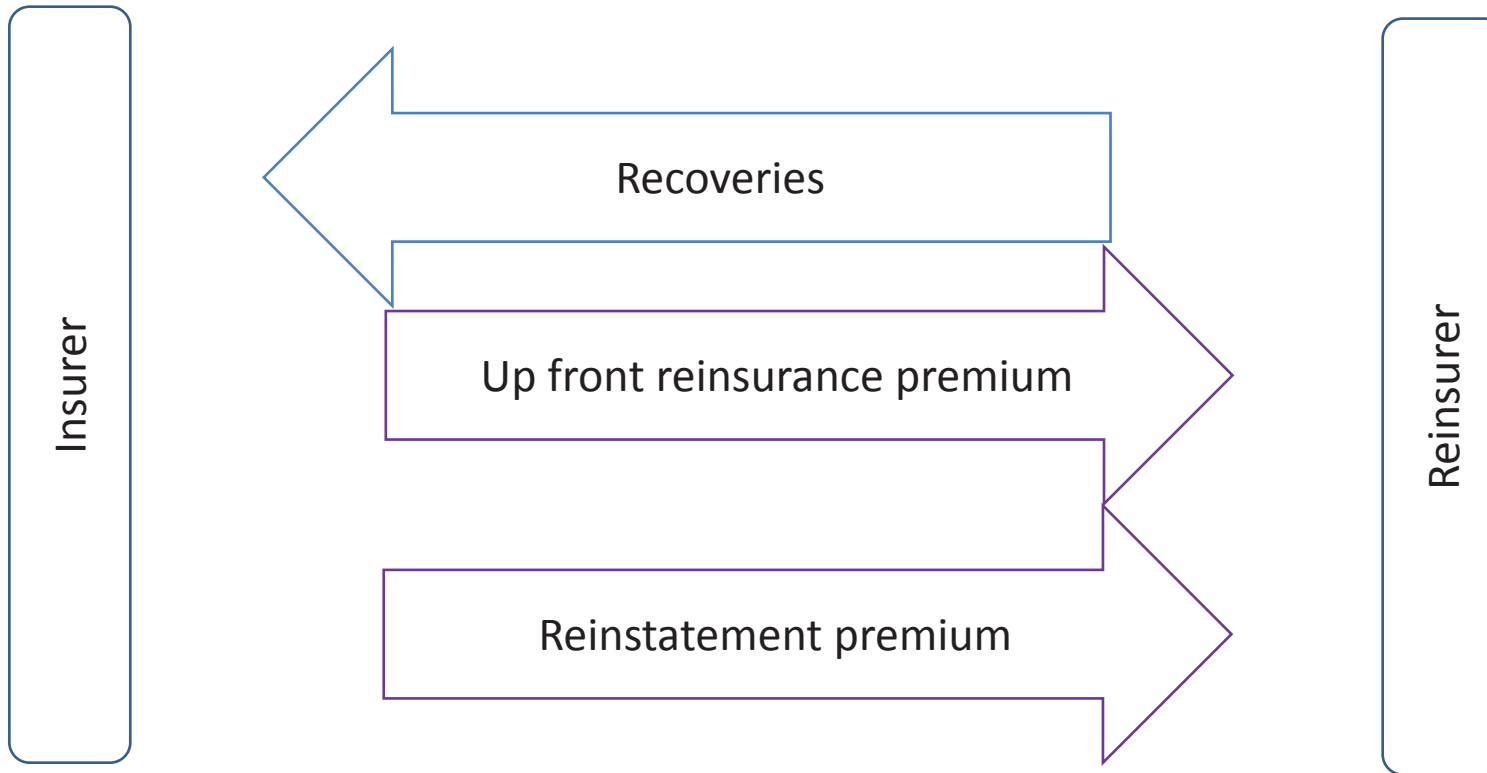
## NON Proportional Reinsurance

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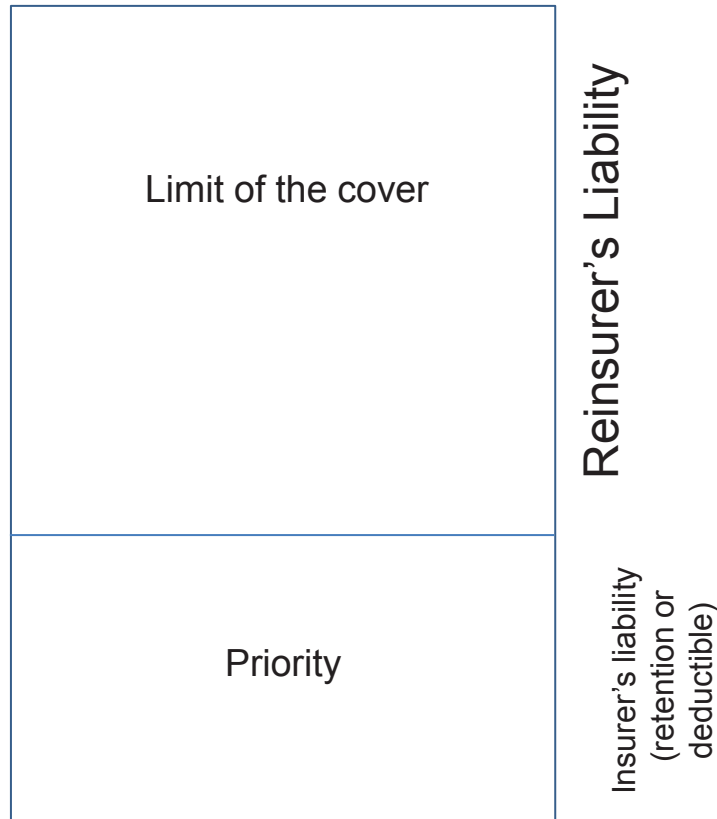
## Cash Flow of Non-Proportional Treaty

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# Excess of Loss Contract Specification (XL, XoL)

For non-proportional reinsurance, liabilities from claims are split between insurer and reinsurer on claim basis, not on sum insured basis, as for proportional treaties. Reinsurer is obliged to pay to insurer the part of the claim which exceeds the pre-agreed amount (deductible, attachment) and up to the limit of the cover.



Limits: Deductible and Cover

**Price :**

1. **Fixed:** is given as % (rate) of the premium exposing the contract (SEPI-subjected estimated premium income)
2. **Variable:** as a % of SEPI but subjected to the excess claim ratio
  - Minimum rate < effective rate < maximum rate
  - Effective rate = recoveries/SEPI multiplied by loading
1. **Flat:** specified in an amount

**Minimum and deposit premium:** % of the price, which is mostly paid in 4 instalments during the year and readjusted to the price after the end of the year (80%-90% of the rate X SEPI) once exact amount of premium is known.

**Reinstatement details specified**

**Annual aggregate limit or annual aggregate deductible specified**

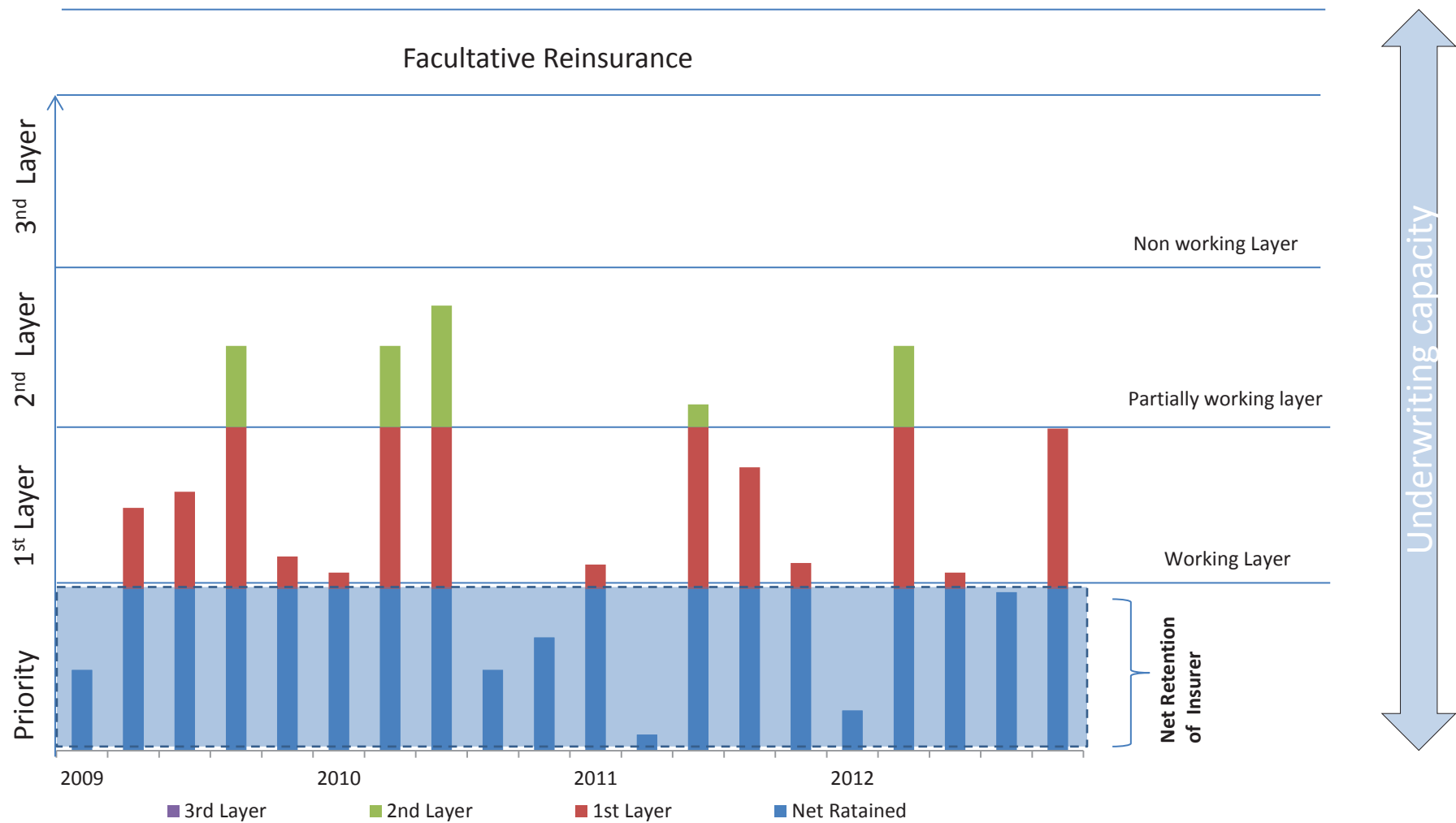
(+) reduction in administration costs, reinsurance premium not calculated on per risk basis but on the cedant's whole portfolio basis

(+) insurer does not cede profitable business to reinsurer, XL works in extreme cases

(-) excess of loss on per risk/per event basis only cover cedant against very large losses

(-) negative cash flow at the beginning of the treaty (one of the function of reinsurance function is to help to start-up underwriting of some class of business, XL not really appropriate)

# Excess of Loss Layering



# Reinstatements

- Limit of the cover protects insurer against the severity of the claim, the frequency of claims is protected by the reinstatement clause
- In the reinsurance contract, **SLIP**, is specified, how many limits and for what price has insurance company available
  1. Unlimited and free (motor third party liability-MTPL)
  2. Limited and free ( MTPL, property per risk)
  3. Limited and paid (property per risk and cat covers)

Reinstatement clause grants the insurer to get/pay for additional cover in case, part or the whole limit was consumed, so the full cover is available for next claim.

## MTPL

Layer 1:	Five full free reinstatements.
Layer 2:	Two full free reinstatements.
Layer 3: Domestic:	Two full free reinstatements.
Green Card:	Unlimited and free.

## Property per risk excess of loss

Article VI	
Reinstatements	
1st Layer:	1 (one) free and 2 (two) at 100% additional premium representing a maximum liability of the Reinsurer of BGN 4,000,000 in all during the term of this Agreement
2nd Layer:	2 (two) at 100% additional premium representing a maximum liability of the Reinsurer of BGN 14,536,215 in all during the term of this Agreement
3rd Layer:	1 (one) at 100% additional premium representing a maximum liability of the Reinsurer of BGN 26,309,190 in all during the term of this Agreement
4th Layer:	1 (one) at 100% additional premium representing a maximum liability of the Reinsurer of BGN 40,000,000 in all during the term of this Agreement
5th Layer:	1 (one) at 100% additional premium representing a maximum liability of the Reinsurer of BGN 138,000,000 in all during the term of this Agreement

# Reinstatement Premium

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In case of paid reinstatement, except of initial premium specified in the contract with the rate (up-front or base premium), additional reinstatement premium is paid during the year

## Pro rata capita

$$\text{reinstatement premium} = \frac{\text{Claim's recoveries from XL}}{\text{Limit}} \times \text{Premium for Layer} \times \% \text{ Reinstatement}$$

## Double pro rata/pro rata temporis

$$\text{reinstatement premium} = \frac{\text{Claim's recoveries from XL}}{\text{Limit}} \times \frac{\text{Number of days to expire}}{365} \times \text{Premium for Layer} \times \% \text{ Reinstatement}$$



# Excess of loss : premium cash flow

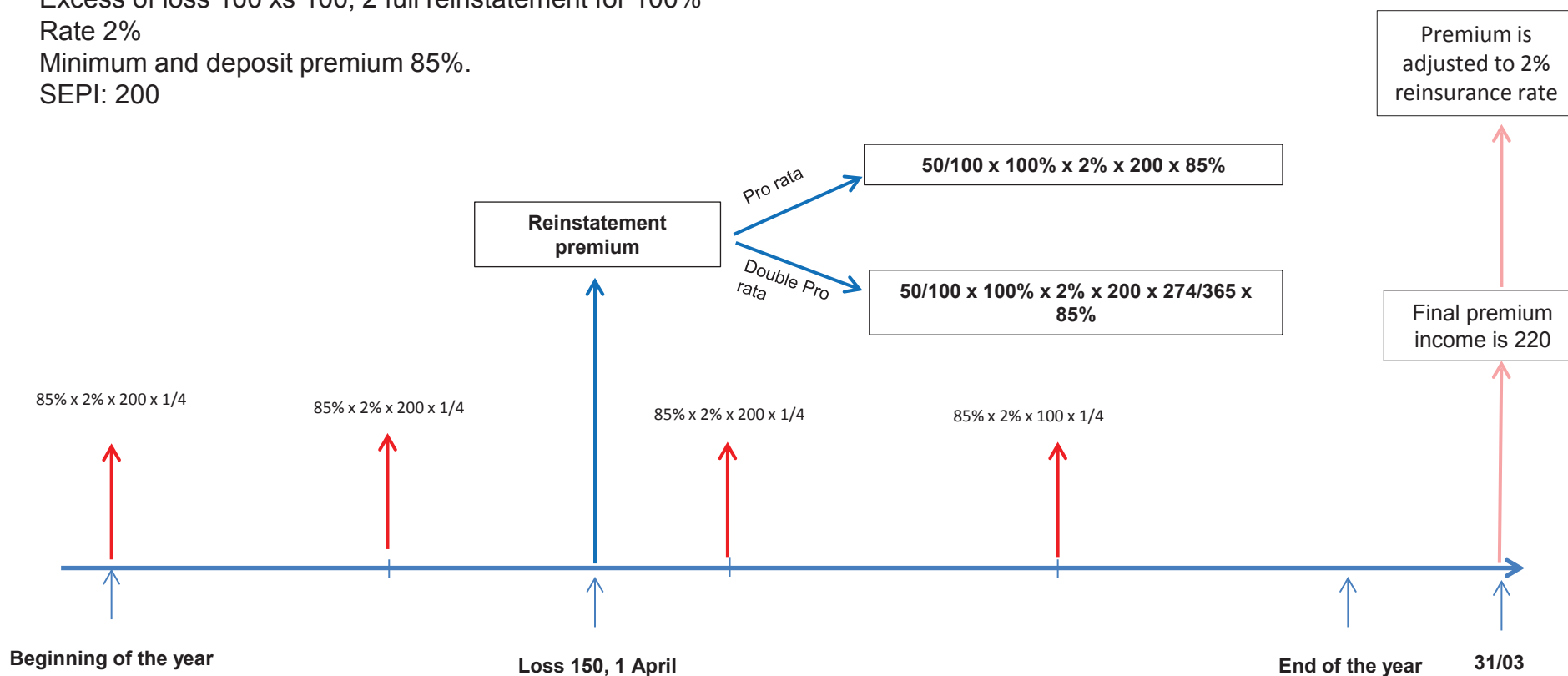
## Contract Details

Excess of loss 100 xs 100, 2 full reinstatement for 100%

Rate 2%

Minimum and deposit premium 85%.

SEPI: 200

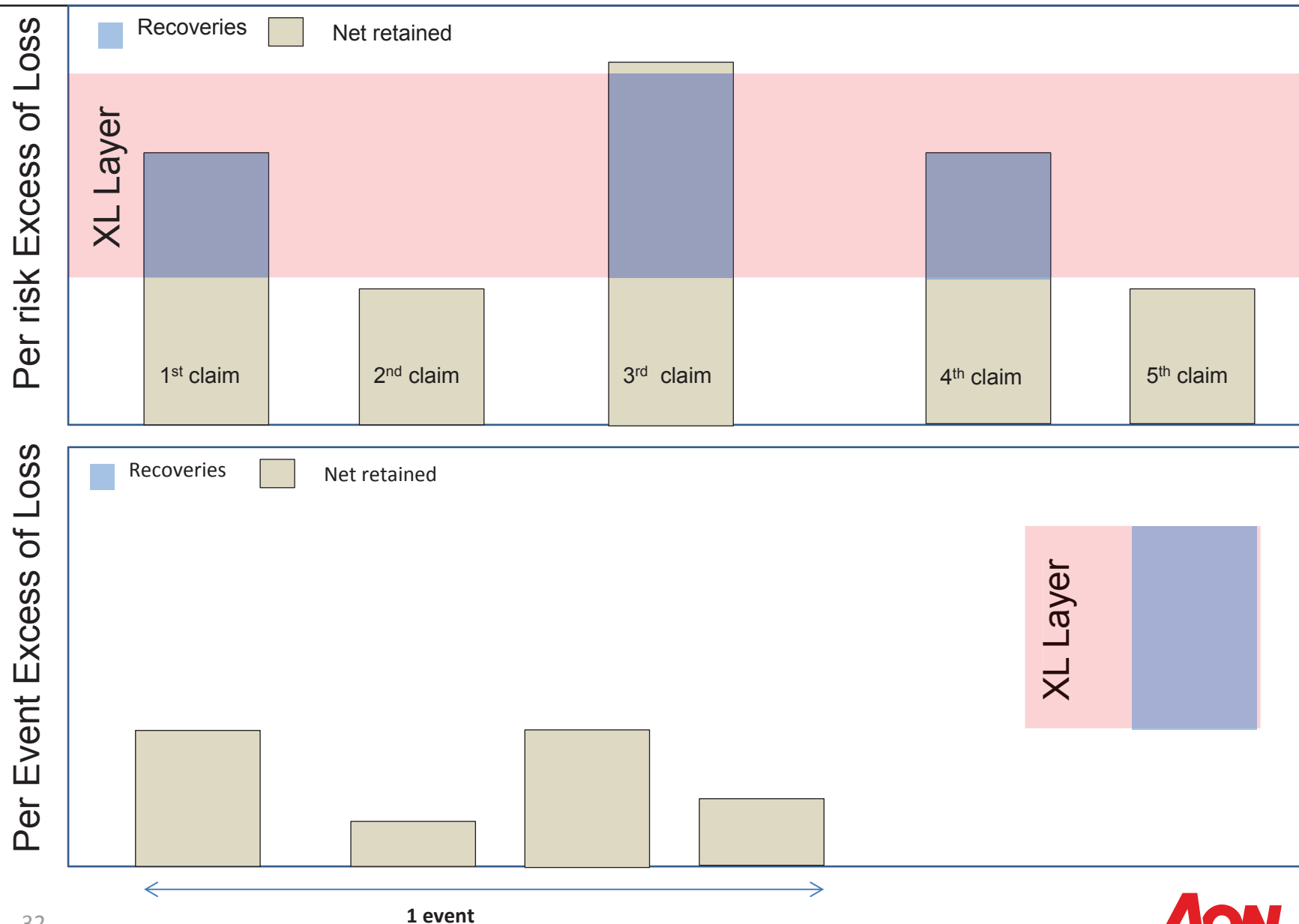


# Reinstatements and impact on XL price



Number and price of reinstatements are important factors in pricing of non proportional treaty

## Excess of loss per risk & per event

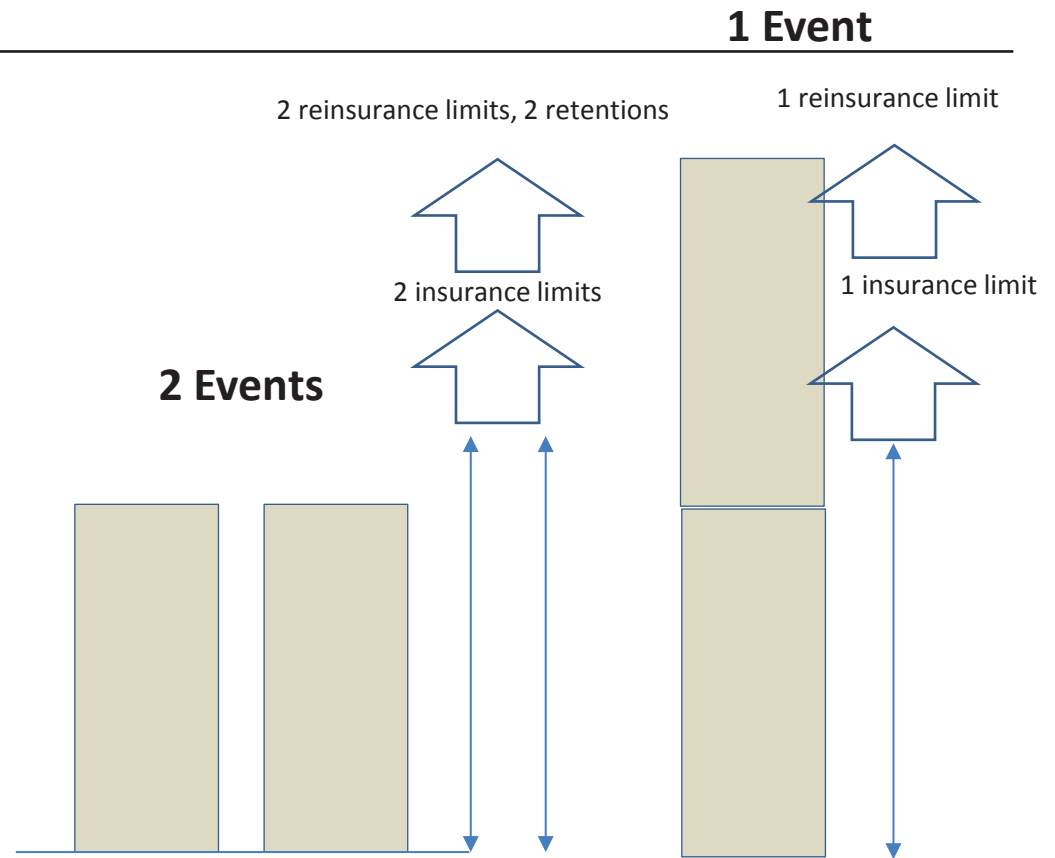


# Why events matters?

## 9/11/2001 Attacks



Source: www.everystockphoto.com



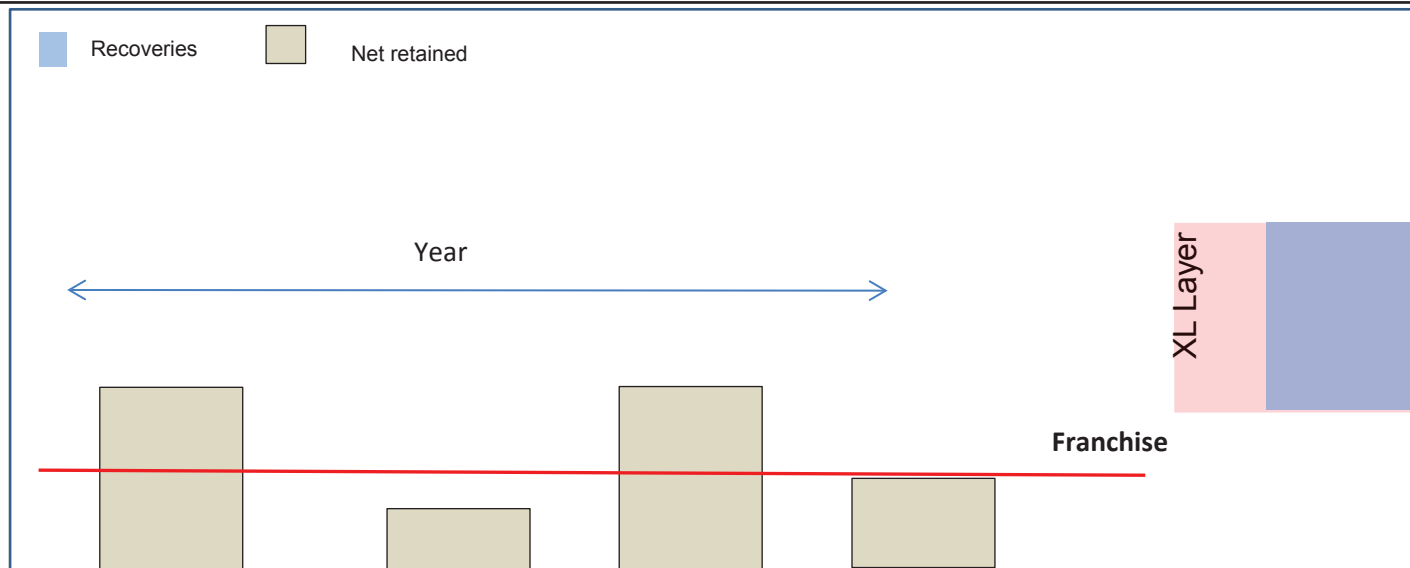
“.....SCOR and its retrocessionnaires will assume, to the extent of their respective commitments, their share in the indemnification obligations relating to the World Trade Center claim. The additional costs resulting from the full coverage **of two distinct events** are estimated to 39 million euros after tax and retrocession...”

Source: www.scors.com, **Press Release**, 13 November 2009

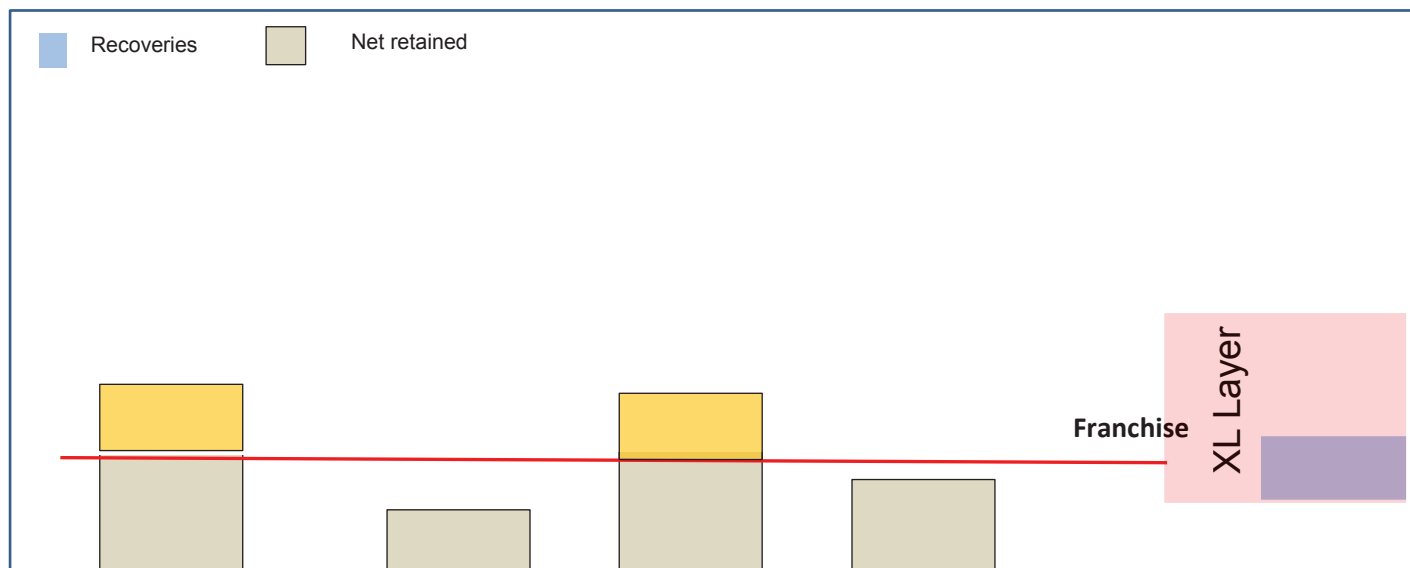
# Stop Loss & Aggregate Cover



# Variation on Aggregate Covers



Only losses excess of franchise are aggregated, they are aggregated from ground up.



Only part of the losses excess of franchise are aggregated.

## Annual Aggregate Deductible (AAD) & Annual Aggregate Cover (AAL)

### Annual Aggregate Deductible (AAD)

Deducted from the total losses ceded to reinsurer (E.g. AAD EUR 1 mio; first 1 mio of recoveries from XL are retained on net retention of insurer)

Union and European Economic Area and their interests abroad.	
Type of Treaty	Per Risk Excess of Loss Contract Losses occurring during basis. Ultimate Net Loss each and every loss each and every Risk
Limit	For 100%: EUR 12,000,000 AAD (Annual Aggregate Deductible) EUR 12,000,000 applies
Retention	For 100%: EUR 8,000,000

### Annual Aggregate Limit (AAL)

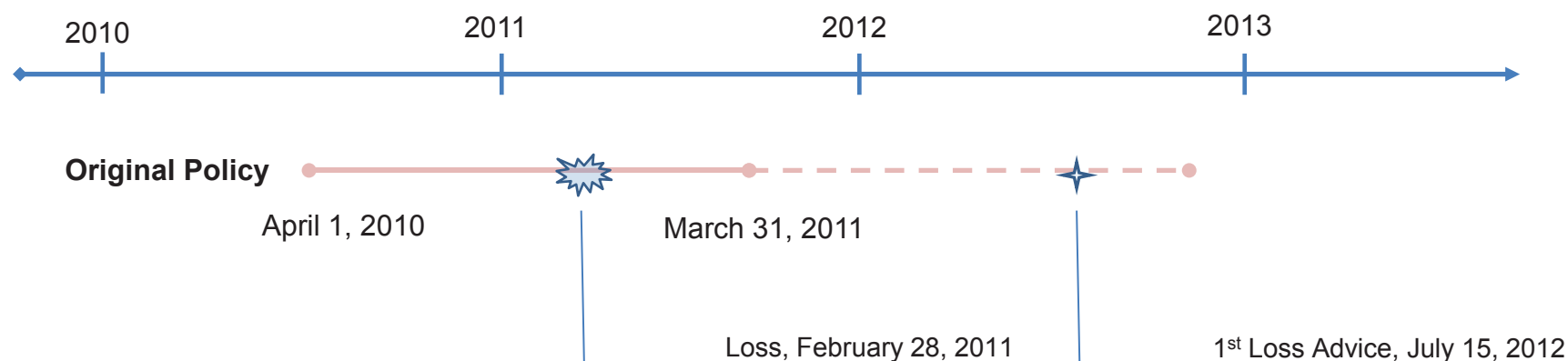
Cover is limited to this amount, it is equivalent of free and limited reinstatements.

The purpose of introduction different features like AAD, franchise or different prices for reinstatements, is to find the right balance between the price of the contract and its function and interaction with the goals of cedant.



# Time Basis of the Contract

- Underwriting Year Basis (Risk Attaching During-RAD or policies incepting during-PID)
- Occurrence Year Basis (Loss Occurring During)
- Claims Made Basis



# Time Basis of the Contract

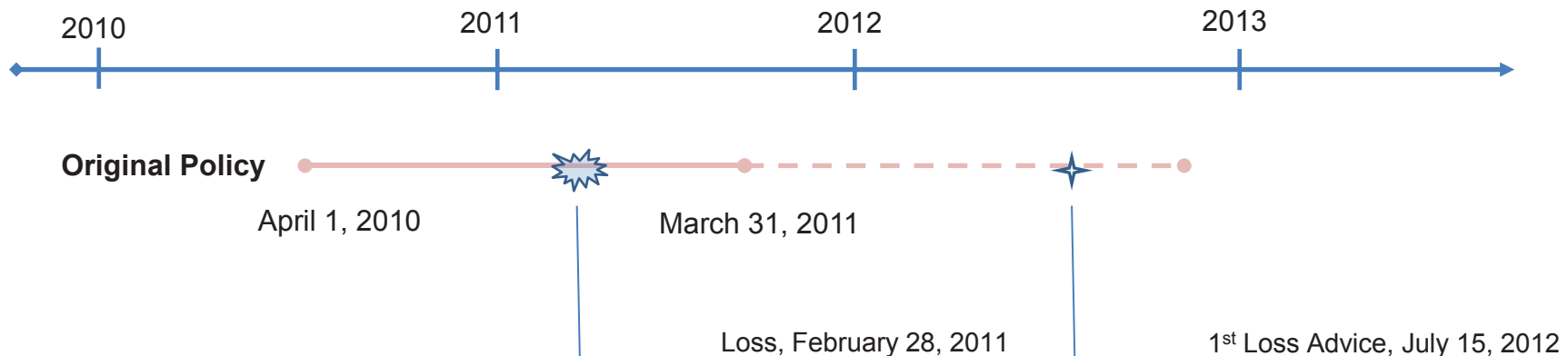
- Underwriting Year Basis (Risk Attaching During-RAD or policies incepting during-PID)
- Occurrence Year Basis (Loss Occurring During)
- Claims Made Basis

as stated in the individual signing pages:

<b>Period</b>	This Contract shall apply to risks attaching during the 12 months period:
Effective from:	1 January 2013
Expiring on:	31 December 2013

Covered by the reinsurance contract

2010



# Time Basis of the Contract

- Underwriting Year Basis (Risk Attaching During-RAD or policies incepting during-PID)
- Occurrence Year Basis (Loss Occurring During)
- Claims Made Basis

## Period

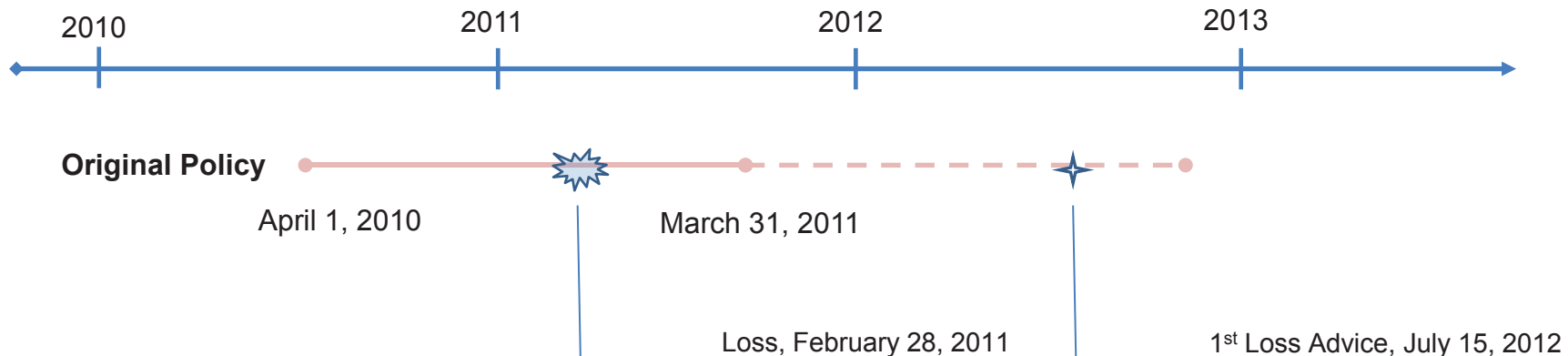
This contract will apply to losses occurring during the following period:

January 1, 2014 (00:00 hrs.) through December 31, 2014 (24:00 hrs.)

Subject to local time at insured property.

Covered by the reinsurance contract

2011

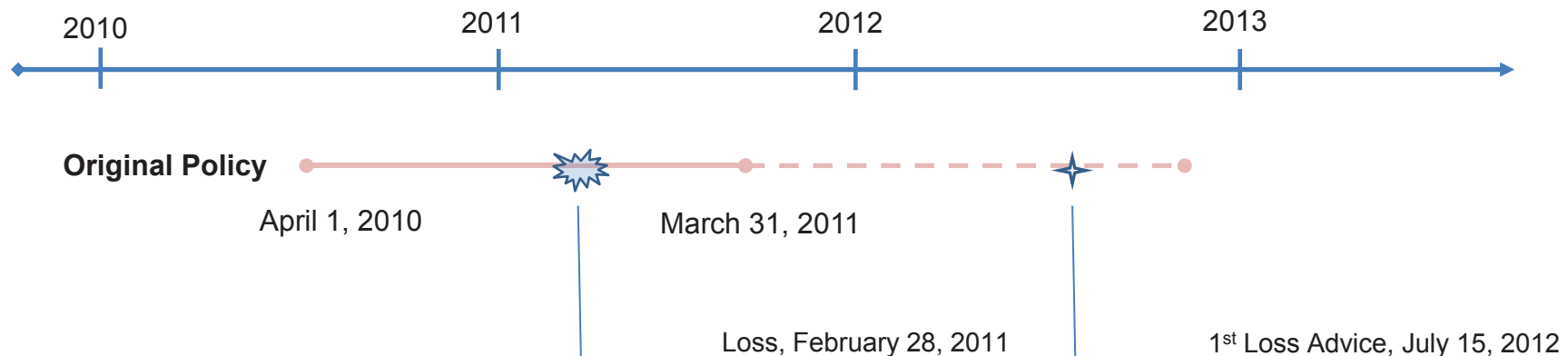


# Time Basis of the Contract

- Underwriting Year Basis (Risk Attaching During-RAD or policies incepting during-PID)
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- Claims Made Basis

Covered by the reinsurance contract

2012



# Some Important Underwriting and Claims Clauses in Reinsurance Agreements

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Because of the wide variety of reinsurance needs, many reinsurance agreements have customized clauses drafted specifically for that reinsurance relationship

## **Stability/Index Clause**

Used for long tail business (MTPL) mostly due the long period between loss occurrence and final settlement. It spreads the impact of inflation equitable between the cedant and reinsurer, refer as *Full Index Clause* and *Severe Index Clause*

## **Hour Clause**

Used for catastrophic covers which limits the time period during which can be claim included to the aggregation to be subjected to cover. The time period is measured in consecutive hours and used mostly in property business for flood, earthquake or windstorm. E.g. 72 consecutive hours regards windstorm or earthquake, 504 consecutive hours regards flood.

The reinsured may choose the date and time when any such period of consecutive hours commences.

## **Interlocking clauses**

Sharing a loss which involves two or more reinsurance treaty, so the cedant does not retain two or more deductibles from one loss.

## **Notification Clause, War Exclusion Clause, Downgrade Clause....**



## Pricing

Empower Results®

**AON** BENFIELD

# Methods for Reinsurance Pricing of Excess of Loss

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1. Experience Analyses (Burning Cost, “as if ” calculation)
2. Exposure Rating
3. Frequency Severity Model
4. Market Benchmarking

# Pricing of Proportional versus Non-Proportional

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- Pricing of non proportional reinsurance focus on estimation of the probabilistic distribution of recoveries from excess of loss contract which leads to the estimation of the **price**

- Price of excess of loss consists from :

Risk premium  
+ Safety margin-loss volatility  
+ Reinsurer's expense  
+ Reinsurer's profit  
+Capital Loading  
Technical Price  
+/-Soft Factors (market trends, reinsurer's panel...)  
**= Market Rate**

- The price of the proportional treaty is specified by the commission paid back by the reinsurer
- Pricing focuses on the determination of expected loss ratio and consequently **combine ratio** (paid losses by reinsurer + commission to insurer) of the treaty
- The philosophy of proportional treaties pricing is similar to pricing of excess of loss



## Data Used for Pricing

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- Premium development
- Number of policies development
- Large losses, losses in excess of threshold (at least 50% of priority)/Triangulations
- Risk Profiles (Snapshot basis or underwriting year basis)
- Information about reinsurance structures historically
- In case of proportional treaties pricing, loss profiles (losses grouped according to SI/PML) for previous year needed (e.g. surplus pricing)
- Large Risks/Facultative Risk
- Historical loss ratios



## Experience Rating

Empower Results®

**AON** BENFIELD

## Experience Rating (Burning cost)

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- Experience analysis focuses on the restatement of all statistics to renewal year context “AS IF” statistics, from economical and portfolio point of view
- Premium re-evaluation  
Premium should be adjusted to current insurance tariff level  
**Index for re-evaluation:** tariff index
- Claims re-evaluation  
Losses should be re-evaluated according to
  - Market factors (economical inflation+ social or legal inflation)
  - Change in the underwriting (do not underwrite some type of risk)
  - Reserving policies (this is applied in MTPL adjustments for IBNeR)**Index for re-evaluation:** inflation (superimposed inflation for MTPL, CPI, wage index, construction index etc.)

# Short Tail and Long Tail Business

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## **Short Tail Business (all types of property business)**

- Inflation is driven by economic factors CPI, wage index, construction index
- Losses are developed in short period of time (1-3 year )
- Possibility to work with last status of losses

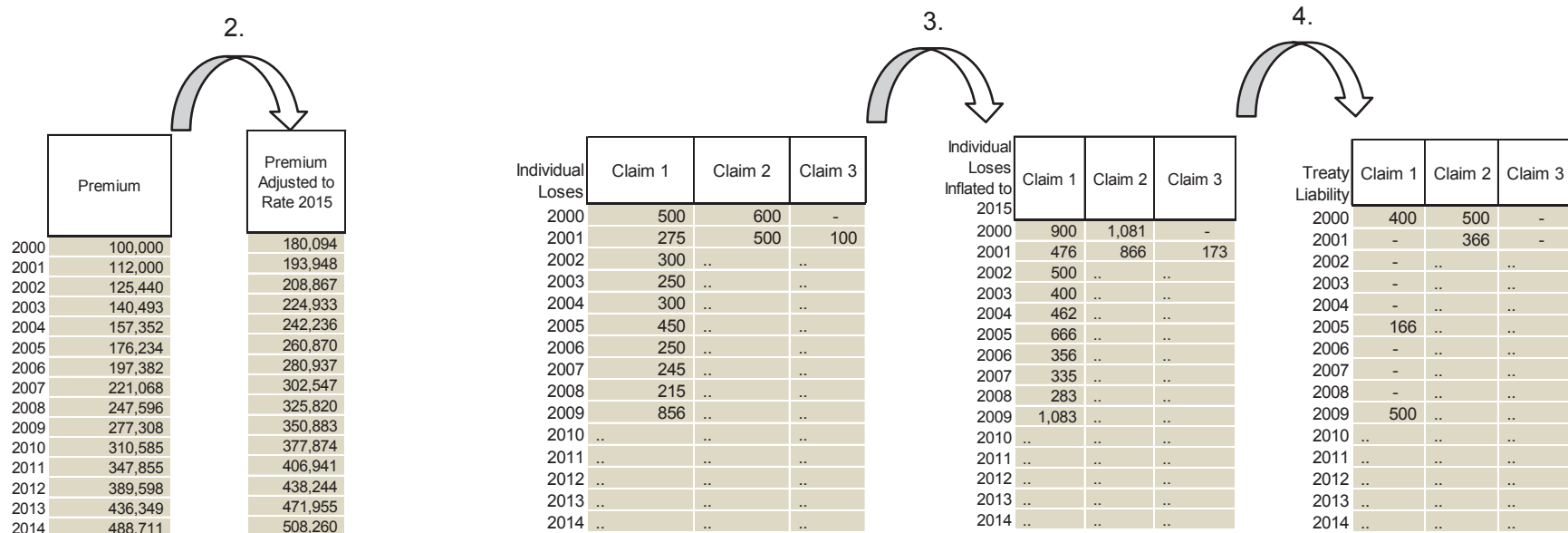
## **Long Tail Business (MTPL, General Third Party Liability)**

- Inflation depends on legal environment, social changes
- Due to the long period between loss occurrence and final settlement FIC and SIC have big impact on the price
- Adjustments on RBNS cause changes in incurred claims (paid amount+reserve)
- It is necessary to work with triangulated claims and use techniques to handle IBNR

# Experience Rating/Burning Cost –Short Tail

## Main Steps

1. Understand of covered risk by the treaty and its functionality (reinstatement, AAD etc.)
2. Projection of premium to renewal year
3. Projection of losses to renewal year
4. Calculated recoveries per claim and cumulate them by year



# Experience Rating/Burning Cost –Short Tail

## Main Steps

1. Understand of covered risk by the treaty and its functionality (reinstatement, AAD etc.)
2. Projection of premium to renewal year
3. Projection of losses to renewal year
4. Calculated recoveries per claim and cumulate them by year
5. Calculate rates per year
6. Average technical rate calculated

	Total Reinsure Liabilities	Premium Adjusted to Rate 2015	Rate
2000	400	180,094	0.2%
2001	-	193,948	-
2002	-	208,867	-
2003	-	224,933	-
2004	-	242,236	-
2005	166	260,870	..
2006	-	280,937	..
2007	-	302,547	..
2008	-	325,820	..
2009	500	350,883	..
2010	..	377,874	..
2011	..	406,941	..
2012	..	438,244	..
2013	..	471,955	..
2014	..	508,260	..

Average 1.50%

Standard Deviation 2.30%

- Pure rate = Average [losses to the layer/ Premium]
- Risk margin and reinsurer's cost loadings need to be added

$$\text{Loaded Rate} = \frac{(\text{Pure Rate} + \text{Volatility Loading} * \text{Volatility})}{(1 - \text{Reinsurer Costs and Profit})}$$

What should be the loading?

# Loadings in Reinsurance

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- Each reinsurer has its own view on loadings, needed to accept XL contract
- Depends on the strategy, market, capital needed to cover the treaty etc.
- **Ways to estimate market loadings (by broker/client)**
  - Estimation from similar contracts on the market (possibility for MTPL, CAT )
  - Market implied loadings from the last year (relation between the last year pure rate and the market price)

# Experience Rating – Long Tail

## Main Steps

1. Understand of covered risk by the treaty and its functionality (reinstatement, AAD etc.)
2. Projection of losses to renewal year (occurrence year or development year method)

Step 2

Country of Company	Company	UY	Country of accident	Date of Loss	Date of 1st Report	Currency for claims in EUR	Reporting Threshold in EUR	domestic	Schedule	31/12/2008	31/12/2009	31/12/2010	31/12/2011	31/12/2012	30/06/2013	30/06/2014
Croatia		2008		19/04/2008	28/05/2008	50,000	GC	paid		9,395	31,931	41,216	41,765	41,848	41,931	41,931
Croatia		2008		19/04/2008	28/05/2008	50,000	GC	outstanding		30,425	9,561	20,703	12,614	7,240	7,157	7,157
Croatia		2008		19/04/2008	28/05/2008	50,000	GC	total incurred		39,820	41,492	61,919	54,379	49,088	49,088	49,088
Croatia		2008		25/04/2008	28/06/2008	50,000	GC	paid		202	425	491	933	2,008	2,008	2,008
Croatia		2008		25/04/2008	28/06/2008	50,000	GC	outstanding		80,228	80,982	220,553	220,110	271,509	271,509	271,509
Croatia		2008		25/04/2008	28/06/2008	50,000	GC	total incurred		80,430	81,407	221,043	221,043	273,517	273,517	273,517
Croatia		2008		14/05/2008	10/07/2008	50,000	GC	paid		0	405	1,554	5,431	5,431	228,994	228,994
Croatia		2008		14/05/2008	10/07/2008	50,000	GC	outstanding		67,027	112,868	213,577	212,974	212,974	0	0
Croatia		2008		14/05/2008	10/07/2008	50,000	GC	total incurred		67,027	113,273	215,130	218,405	218,405	228,994	228,994
Croatia		2008		16/03/2009	24/03/2009	50,000	GC	paid		0	1,911	3,286	67,044	86,227	86,227	86,227
Croatia		2008		16/03/2009	24/03/2009	50,000	GC	outstanding		0	229,102	255,991	200,033	0	0	0
Croatia		2008		16/03/2009	24/03/2009	50,000	GC	total incurred		0	231,013	258,377	267,077	86,227	86,227	86,227
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Croatia		2008		28/05/2008	24/10/2008	50,000	GC	outstanding		46,696	46,635	72,689	72,553	48,083	36,219	36,219
Croatia		2008		28/05/2008	24/10/2008	50,000	GC	total incurred		47,347	47,609	74,029	74,029	86,655	92,322	92,322
Croatia		2008		31/10/2008	08/12/2008	50,000	GC	paid		0	1,051	101,992	101,992	101,992	101,992	101,992
Croatia		2008		31/10/2008	08/12/2008	50,000	GC	outstanding		32,409	78,984	0	0	0	0	0
Croatia		2008		31/10/2008	08/12/2008	50,000	GC	total incurred		32,409	80,035	101,992	101,992	101,992	101,992	101,992
Croatia		2008		26/05/2008	19/01/2009	50,000	GC	paid		0	493	1,214	2,588	59,288	59,288	59,288
Croatia		2008		26/05/2008	19/01/2009	50,000	GC	outstanding		0	53,359	52,638	78,419	0	0	0
Croatia		2008		26/05/2008	19/01/2009	50,000	GC	total incurred		0	53,852	53,852	81,008	59,288	59,288	59,288
Croatia		2008		27/10/2008	28/01/2009	50,000	GC	paid		0	710	41,298	59,081	59,081	59,081	59,081
Croatia		2008		27/10/2008	28/01/2009	50,000	GC	outstanding		0	32,289	2,516	133	0	0	0
Croatia		2008		27/10/2008	28/01/2009	50,000	GC	total incurred		0	32,999	43,814	59,214	59,081	59,081	59,081
Croatia		2009	Germany	13/02/2009	26/02/2010	50,000	GC	paid		0	0	75,613	76,804	76,804	76,804	76,804

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Croatia		2008		31/10/2008	08/12/2008	50,000	GC	outstanding		32,409	78,984	0	0	0	0	0
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Croatia		2009	Germany	13/02/2009	26/02/2010	50,000	GC	paid		0	0	75,613	76,804	76,804	76,804	76,804



# Experience Rating – Long Tail

## Main Steps

1. Understand of covered risk by the treaty and its functionality (reinstatement, AAD etc.)
2. Projection of losses to renewal year (occurrence year or development year method)
3. Losses adjusted for IBNeR, on per loss basis (adjustment for under reserving or over reserving)

Step 3

Country of Company	Company	UY	Country of accident	Date of Loss	Date of 1st Report	Currency for claims in EUR	Reporting Threshold in EUR	domestic	Schedule	31/12/2008	31/12/2009	31/12/2010	31/12/2011	31/12/2012	30/06/2013	30/06/2014
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Croatia		2008		26/05/2008	19/01/2009	50,000	GC	total incurred		0	53,852	53,852	81,008	59,288	59,288	59,288
Croatia		2008		27/10/2008	28/01/2009	50,000	GC	paid		0	710	41,298	59,081	59,081	59,081	59,081
Croatia		2008		27/10/2008	28/01/2009	50,000	GC	outstanding		0	32,289	2,516	133	0	0	0
Croatia		2008		27/10/2008	28/01/2009	50,000	GC	total incurred		0	32,999	43,814	59,214	59,081	59,081	59,081
Croatia		2009	Germany	13/02/2009	26/02/2010	50,000	GC	paid		0	0	75,613	76,804	76,804	76,804	76,804

# Experience Rating – Long Tail

## Main Steps

1. Understand of covered risk by the treaty and its functionality (reinstatement, AAD etc.)
2. Projection of losses to renewal year (occurrence year or development year method)
3. Losses adjusted for IBNeR, on per loss basis (adjustment for under reserving or over reserving)
4. Application of the layer
5. Aggregation of losses on per treaty year basis

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
2000	0	0	0	76,124	63,506	51,354	39,653	28,386	5,620	10,203	0	31,679	31,679	42,565	42,565
2001	0	0	0	0	0	0	0	0	49,120	25,952	13,312	0	0	0	0
2002	0	369,801	399,164	396,363	477,031	438,105	537,451	526,642	1,298,302	1,334,224	1,470,520	1,441,020	1,430,266	0	0
2003	0	0	14,356	65,229	210,623	33,216	0	0	0	0	0	0	0	0	0
2004	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2005	0	0	105,292	97,008	265,675	310,538	294,083	476,628	507,875	507,875	0	0	0	0	0
2006	0	84,587	249,347	223,038	326,214	294,260	310,972	440,267	440,267	0	0	0	0	0	0
2007	0	221,876	744,044	1,099,853	885,694	674,646	929,943	929,943	0	0	0	0	0	0	0
2008	0	232,116	216,782	250,250	298,719	288,506	288,506	0	0	0	0	0	0	0	0
2009	0	0	186,439	332,169	312,055	306,194	0	0	0	0	0	0	0	0	0
2010	0	82,854	81,922	72,199	72,199	0	0	0	0	0	0	0	0	0	0
2011	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2012	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2013	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2014	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0


?

# Experience Rating – Long Tail

## Main Steps

1. Understand of covered risk by the treaty and its functionality (reinstatement, AAD etc.)
2. Projection of losses to renewal year (occurrence year or development year method)
3. Losses adjusted for IBNeR, on per loss basis (adjustment for under reserving or over reserving)
4. Application of the layer
5. Aggregation of losses on per treaty year basis
6. Development to ultimate (chain ladder, B-F ..)

Step 6



	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Ultimate
2000	0	0	0	76,124	63,506	51,354	39,653	28,386	5,620	10,203	0	31,679	31,679	42,565	42,565	42,565
2001	0	0	0	0	0	0	0	0	49,120	25,952	13,312	0	0	0	0	490,944
2002	0	369,801	399,164	396,363	477,031	438,105	537,451	526,642	1,298,302	1,334,224	1,470,520	1,441,020	1,430,266	0	0	476,755
2003	0	0	14,356	65,229	210,623	33,216	0	0	0	0	0	0	0	0	0	476,755
2004	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	476,755
2005	0	0	105,292	97,008	265,675	310,538	294,083	476,628	507,875	507,875	0	0	0	0	0	169,292
2006	0	84,587	249,347	223,038	326,214	294,260	310,972	440,267	440,267	0	0	0	0	0	0	316,047
2007	0	221,876	744,044	1,099,853	885,694	674,646	929,943	929,943	0	0	0	0	0	0	0	626,028
2008	0	232,116	216,782	250,250	298,719	288,506	288,506	0	0	0	0	0	0	0	0	552,905
2009	0	0	186,439	332,169	312,055	306,194	0	0	0	0	0	0	0	0	0	508,214
2010	0	82,854	81,922	72,199	72,199	0	0	0	0	0	0	0	0	0	0	222,300
2011	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	126,131
2012	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	94,598
2013	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	18,050
2014	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

# Experience Rating – Long Tail

## Main Steps

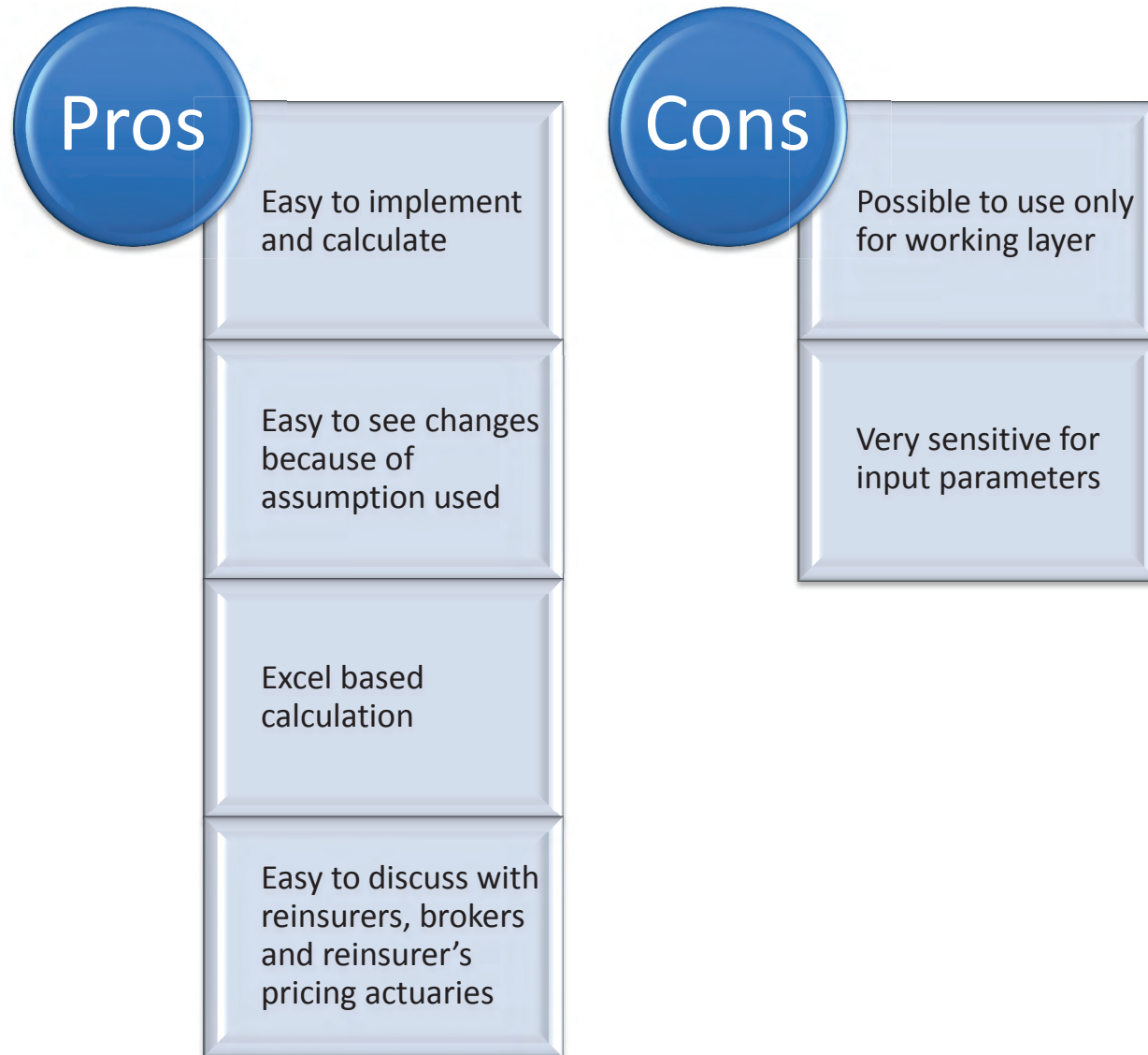
1. Understand of covered risk by the treaty and its functionality (reinstatement, AAD etc.)
2. Projection of losses to renewal year (occurrence year or development year method)
3. Losses adjusted for IBNeR, on per loss basis (adjustment for under reserving or over reserving)
4. Application of the layer
5. Aggregation of losses on per treaty year basis
6. Development to ultimate (chain ladder, B-F ..)
7. Adjustment for exposure
8. Calculated average loss
9. **Average technical rate calculated**

Ultimate	Vehicles	Ultimate Adjuste to Exposure
42,565	3,085,701	104,871
490,944	3,924,352	951,089
476,755	4,445,372	815,352
476,755	5,217,020	694,754
169,292	6,709,466	191,825
316,047	7,079,810	339,382
626,028	7,095,573	670,755
552,905	8,161,852	515,015
508,214	8,541,653	452,338
222,300	8,252,642	204,788
126,131	8,120,199	118,090
94,598	8,574,688	83,873
18,050	7,972,699	17,212
0	7,602,522	0
avg '00-'14		396,873
avg '05-'14		328,803
avg '08-'14		294,582

No index clause and discount benefit applied

# Experience Rating Pros and Cons

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## Exposure Rating

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# Exposure Rating

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## **This method combines**

- Exposure of insurance company, represented by risk profile
- Market distribution of losses in the relation to sum insured/PML-damage ratio

This method is used for the pricing of layer with limited or no loss experience and it's validated on lower layers with some experience or even on artificial layers with lower attachments.

# Exposure Rating

---

We consider an individual risk of insurance portfolio I. Under the assumption of Collective Risk Model, risk i has total claims

$S_i = \sum_{n=1}^{N_i} X_{in}$ , where  $N_i$  is number of claims, independent claim sizes  $X_{i1}, X_{i2} \dots$  with distribution function  $F_{X_i}(x_i) = P(X_{in} \leq x)$

So unlimited excess of loss cover with retention  $a$  pays

$$R = \sum_{i=1}^I \sum_{n=1}^{N_i} \max(X_{in} - a, 0)$$

So the price of such a layer is expected value of recoveries from the layer

$$\begin{aligned} E(R) &= \sum_{i=1}^I E(N_i) E(\max(X_i - a, 0)) \\ &= \sum_{i=1}^I \frac{E(N_i) E(\max(X_i - a, 0))}{E(N_i) E(X_i)} E(S_i) \\ &= \sum_{i=1}^I (1 - r_i(a)) E(S_i) \end{aligned}$$

Where  $r_i(a) := \frac{E(\min(X_i, a))}{E(X_i)}$ , which we call loss elimination function.



# Exposure curve

---

Sum insured of the risk  $i$ :  $SI_i$

Cumulative density function of so called loss degrees:  $G_{Y_i}(y_i)$  where  $Y_i = \frac{X_i}{SI_i}$

Reinsurance policy attachment/deductible:  $a$

Normalized attachment:  $a' := \frac{a}{SI_i}$

Limited expected value:  $L(a') := E[\min(Y, a')] = \int_0^{a'} (1 - G_{Y_i}(y_i)) dy_i$

Using notation above loss elimination function can be expressed as

$$\begin{aligned} r_i(a) &= \frac{E(\min(X_i, a)) \frac{1}{SI}}{E(X_i) \frac{1}{SI}} \\ &= \frac{E(\min(Y_i, a'))}{E(Y_i)} \\ &= \frac{L(a')}{L(1)} = \frac{\int_0^{a'} (1 - G(y_i)) dy_i}{E[Y_i]} \text{ for } 0 \leq a_N \leq 1, \text{ and } r(a_N) := 1 \text{ for } a_N \geq 1 \end{aligned}$$

$\frac{L(a')}{L(1)}$  expresses the ratio of expected loss below some normalized attachment  $a'$ .

The curve representing the function  $r_i(a')$ , for  $0 \leq a' \leq 1$ , is **called exposure curve**.

# Exposure Rating

---

We consider an individual risk of insurance portfolio I. Under the assumption of Collective Risk Model, risk i has total claims

$S_i = \sum_{n=1}^{N_i} X_{in}$ , where  $N_i$  is number of claims, independent claim sizes  $X_{i1}, X_{i2} \dots$  with distribution function  $F_{X_i}(x_i) = P(X_{in} \leq x)$

So unlimited excess of loss cover with retention a pays

$$R = \sum_{i=1}^I \sum_{n=1}^{N_i} \max(X_{in} - a, 0)$$

So the price of such a layer is expected value of recoveries from the layer

$$\begin{aligned} E(R) &= \sum_{i=1}^I E(N_i) E(\max(X_i - a, 0)) \\ &= \sum_{i=1}^I \frac{E(N_i) E(\max(X_i - a, 0))}{E(N_i) E(X_i)} E(S_i) \\ &= \sum_{i=1}^I (1 - r_i(a)) E(S_i) \end{aligned}$$

Where  $r_i(a) := \frac{E(\min(X_i, a))}{E(X_i)}$ , which we call loss elimination function.

# Exposure Rating with Risk Profile

Exposure rating is done on the whole risk profile of the company.

Risk Profile[EUR]		Number of Risk	Average PML	Premium
PML Bands				
From	To			
0	500,000	33,115	174,009	19,840,536
500,001	1,000,000	7,157	716,716	9,412,636
1,000,001	2,000,000	5,258	1,378,240	9,737,979
2,000,001	3,000,000	2,318	2,411,307	6,026,499
3,000,001	4,000,000	1,327	3,425,731	3,838,770
4,000,001	5,000,000	915	4,445,339	3,263,997
5,000,001	7,500,000	1,269	6,023,954	5,210,542
7,500,001	10,000,000	724	8,755,842	3,757,048
10,000,001	15,000,000	530	11,987,695	3,029,078
15,000,001	20,000,000	213	17,280,938	1,442,475
20,000,001	30,000,000	293	25,207,972	1,734,577
30,000,001	40,000,000	108	33,758,063	812,326
40,000,001	50,000,000	15	44,019,305	659,454
50,000,001	80,000,000	10	62,125,636	1,394,822
80,000,001	100,000,000	2	88,788,568	664,500
100,000,001	125,000,000	3	111,557,792	695,844
125,000,001	Higher	1	172,409,284	1,389,326

# Exposure curves

- On the reinsurance market Swiss re curves are used as a standard approach

## Other curves

- Lloyds
- Salzmann (1960 INA Homeowners data)
- ReinsurerCurves (Swiss Re, Munich Re, etc)
- Ludwig (1984-1988 Homeowners and Small Commercial data)
- ISO's PSOLD (Recent Commercial data)

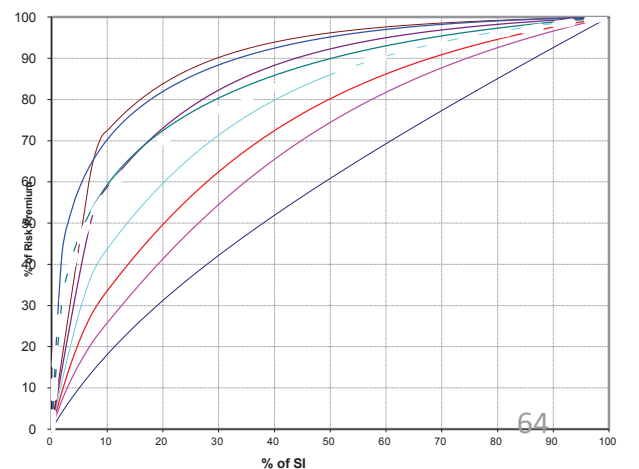
Swiss Re curves are defined by the Y parameters from 0 to 15

- Increasing parameter implies more concave curve and so the lower probability of total loss
- According to the type of risk the right curve should be chosen

Limitation of exposure curves is that these curves were estimated on the market portfolios, so do not have to be accurate and give reasonable results on analysed portfolio.

## Two ways to check

1. Validate on loss profile of the company
2. Validation on working layers (amount of losses to the layer implied by the curve)



# Example: Frequency and Severity implied by Exposure curve

Risk profile:

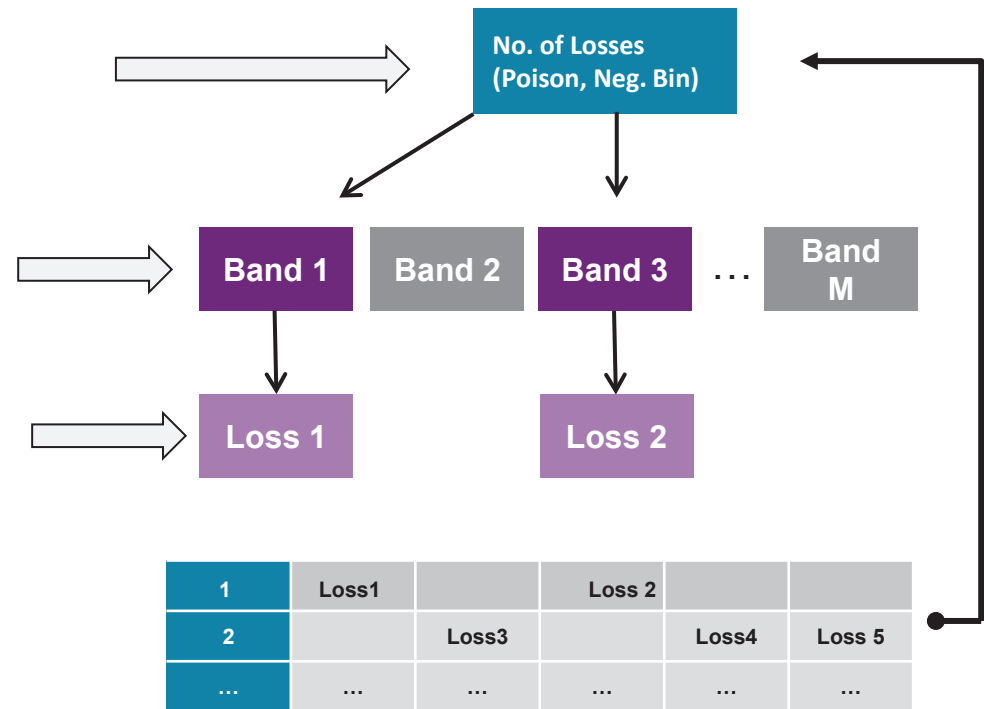
Band From	Band To	Average SI	Premium	Gross LR	Losses
75,000	150,00	102,172	231,018	30%	69,305
...	...	...	...	...	...

Large loss threshold: **50,000**

- For every band in risk profiles  $i$  calculate
  1. Expected average loss per band  $E(AL_i)$  as a mean of severity distribution function applied for given band, i.e.  $E(X) \times \text{Avg. SI}$ 
    - For example, average loss from exposure curve is estimated as 3.21% of SI, so  $102,172 \times 3.21\% = 3,281$  average loss for given band
  2. Total expected losses per band  $E(TL_i)$  as  $\text{Gross LR} \times \text{Premium}$  in given band
    - In this example band  $231,018 \times 30\% = 69,305$
  3. Expected number of losses per band is then total expected losses divided by average loss per band  $n_i = \frac{E(TL_i)}{E(AL_i)}$ 
    - $n_i = \frac{E(TL_i)}{E(AL_i)} = \frac{69,305}{3,281} = 21,12$  – average frequency
  4. Frequency of large losses excess threshold is derived from severity distribution function applied for given band:  $n_i' = P(X > \text{threshold})$ 
    - $n_i' = 21,12 \times P(X > 50,000) = 21.12 \times 0.0129 = 0.273$
- Total frequency of large losses excess threshold is then total frequency of large losses for all bands in risk profile  $N = \sum_{i=1}^M n_i'$

# Monte Carlo Simulation

1. Draw a random number from frequency distribution implied by risk profile and Exposure curve
2. For every loss draw a random number to allocate it stochastically to band (premium or number of policies can be used as a weight)
3. For each loss allocated to band draw a random number from severity distribution in given band implied by exposure curve and risk profile
4. Save result and repeat simulation





## Frequency Severity Rating

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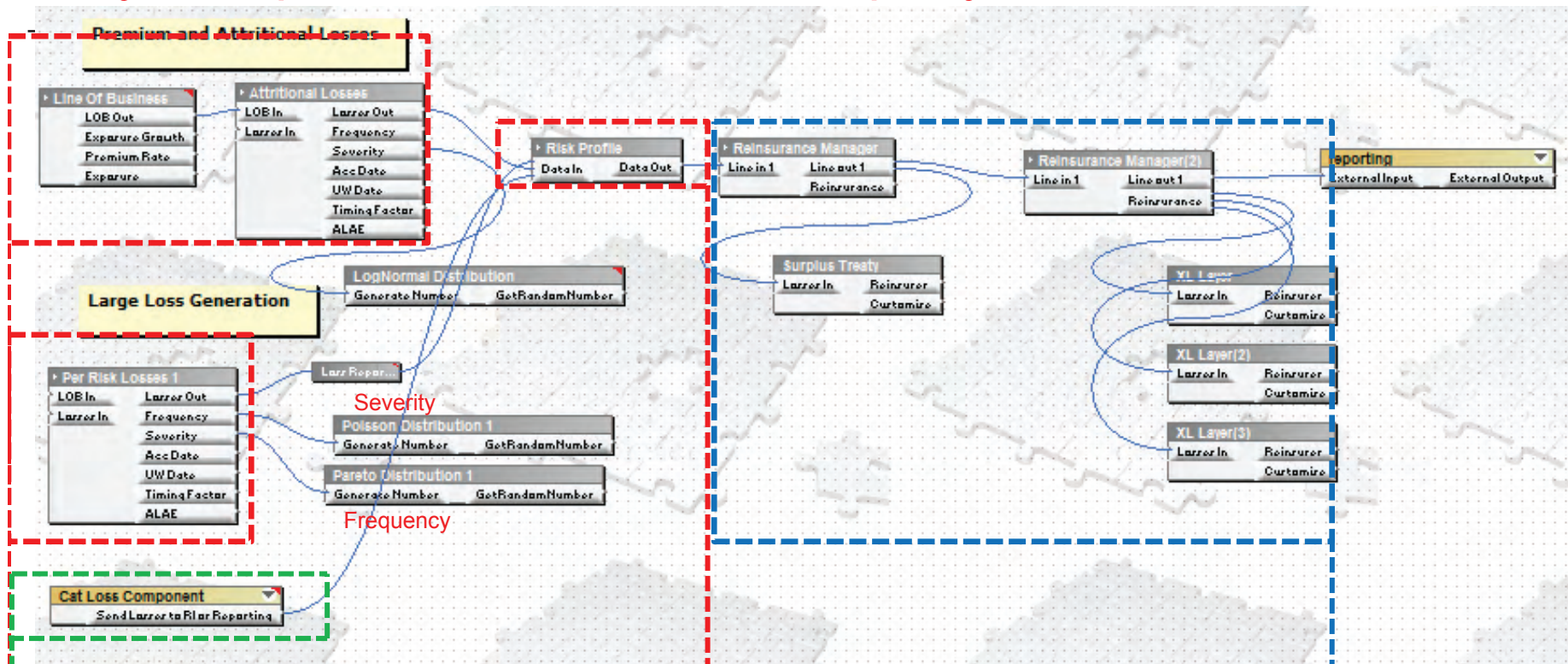
# Frequency Severity Rating

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- By the frequency severity rating method, we mean practise of developing a stochastic model of the insurance portfolio, on which is applied desired reinsurance structure
- It is the mixture between experience rating and exposure
- Key inputs and assumptions can be from the cedant's portfolio or from the market data
  - Typical example is frequency of large losses excess of modelling threshold in MTPL modelling or payment pattern of large losses took from the market
- Simulation can be done
  - Excel spreadsheet with some addins
  - Specialized tool for DFA (dynamical financial analyses) (Remetrica, Igloo...)
- Extremely useful is to build model for pricing and use this model subsequently for the evaluation of reinsurance structure and its optimization
- Stochastic models are extremely useful when complicated reinsurance structures are applied with different clauses, so we can evaluate each claim and its impact to reinsurance
- Retrocession and possible accumulation from correlated risks can be captured via stochastic models
- For the reinsurers, stochastic model is inevitable, because their pricing can be based on the **Risk Based Capital** method, the new treaty contribution to its capital requirement (e.g. TVaR of the whole portfolio and TVaR of the new treaty priced )



# Key Components of Standard Property Model



## Loss generation is mostly split into

- Attrition losses (small losses)
- Large Losses (losses excess threshold)

## Risk Profile

- Possibility to directly generate losses from risk profile via the exposure curve
- Possibility to assign SI to losses, in case of surplus is modelled

## Catastrophic Losses

Generated from outputs from Cat models provider (Impact Forecasting-AB,RMS,...)

## Reinsurance Structure

- Possibility to apply different structures and see the impact on key metrics



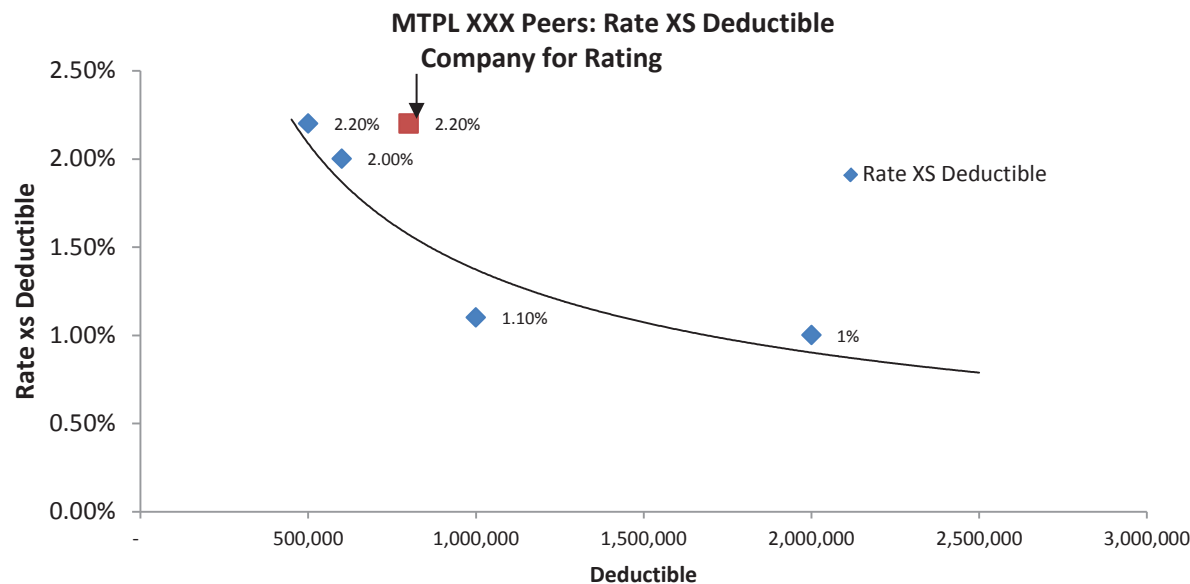
## Market Peers Comparison

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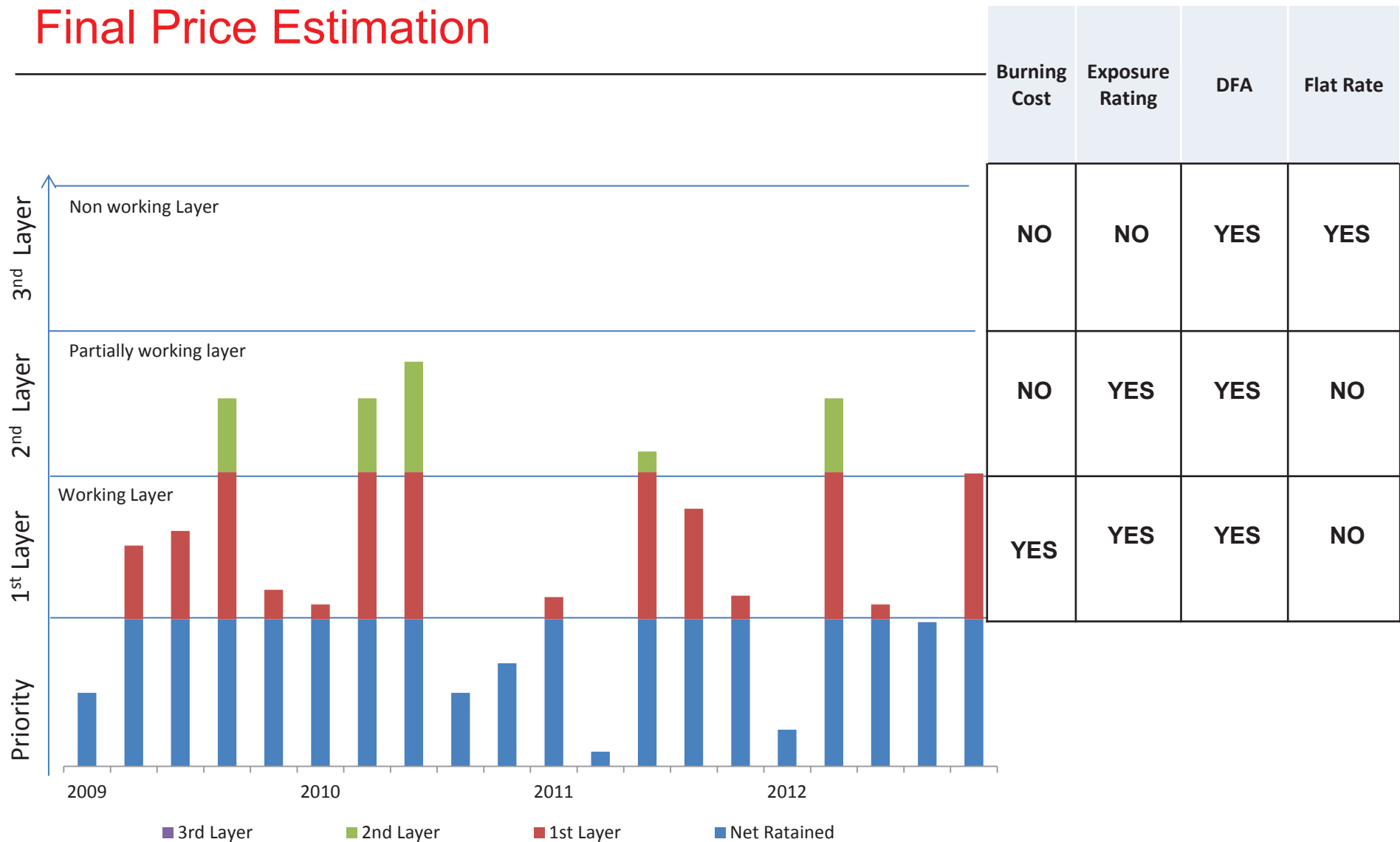
# Market Comparison

- Market comparison can serve as a good reasonability check of technical pricing (burning cost, exposure, DFA)
- Brokers have possibility to see prices on the market
- It works very well for
  - MTPL (possibility to use Generalized non-linear Quasi likelihood approach\*)
  - Cat XL



\*Benchmark Rates for Excess of Loss Reinsurance Program, Verlaak, Hurlimann, Beirlant, 2005

# Final Price Estimation



- First working layers are usually priced on the burning cost basis purely
- Top layers are very often only for capacity purposes and are charged by flat market rate

## Why my quotes differs from reinsurer quotations?

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- Different assumptions (superimposed inflation, discount rate)
- Lead underwriter have different subjective assessment of the risk
- Market cycles hard and soft market
- Strategic/commercial purposes in pricing
- Underwriter/pricing actuary did not consider some information from local market



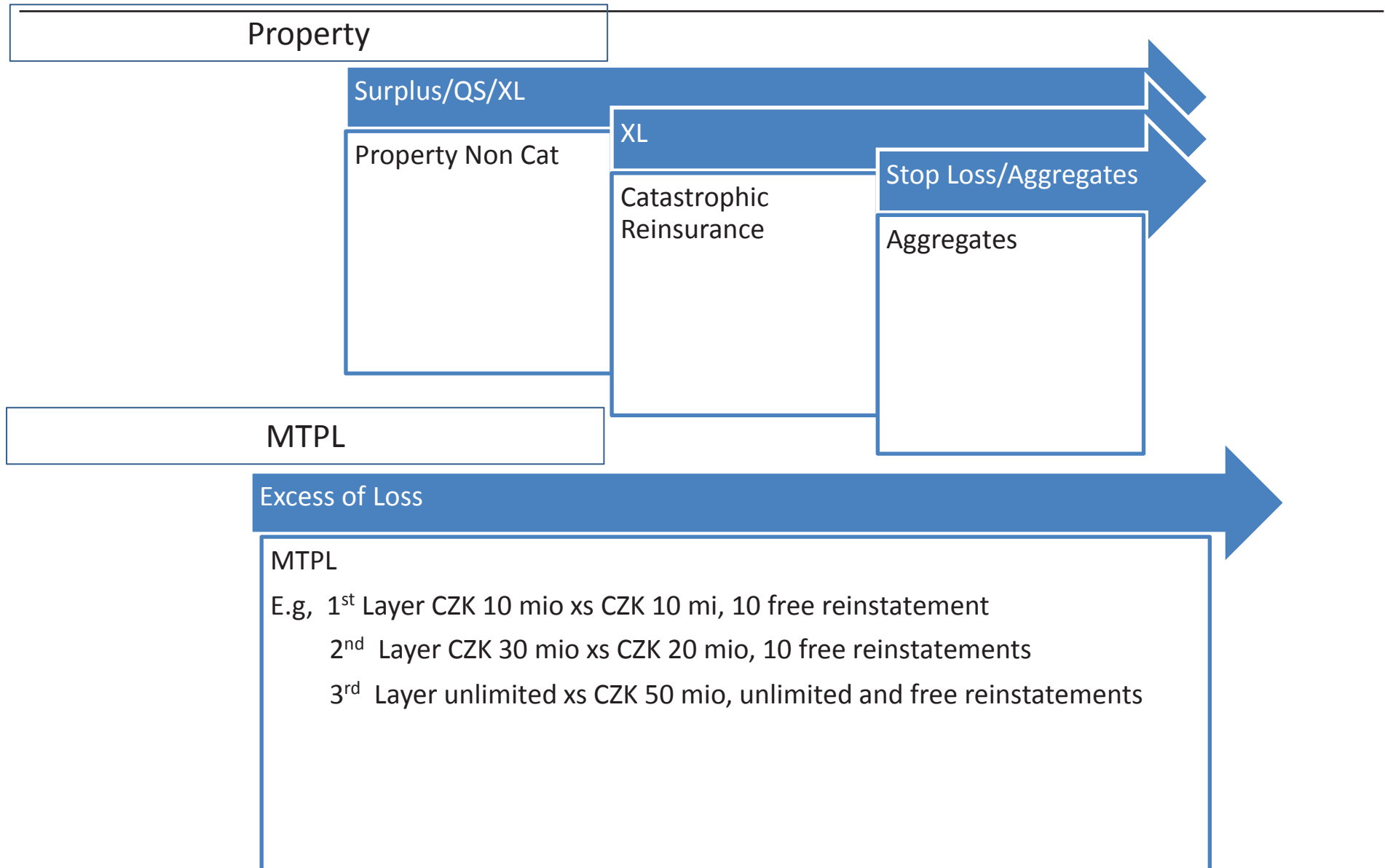
## Reinsurance Structures and New Trends

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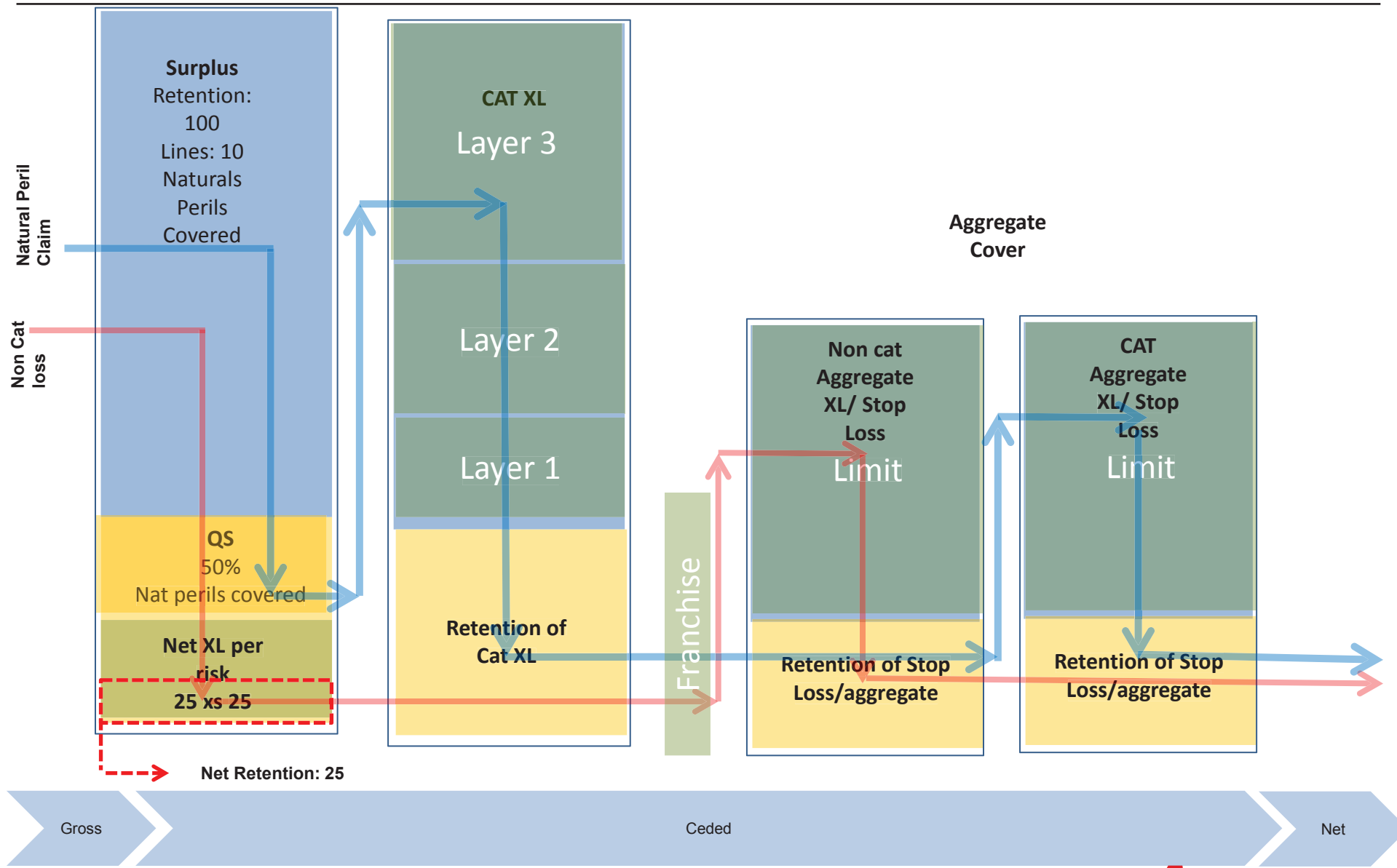
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# Typical Structures for Property & MTPL

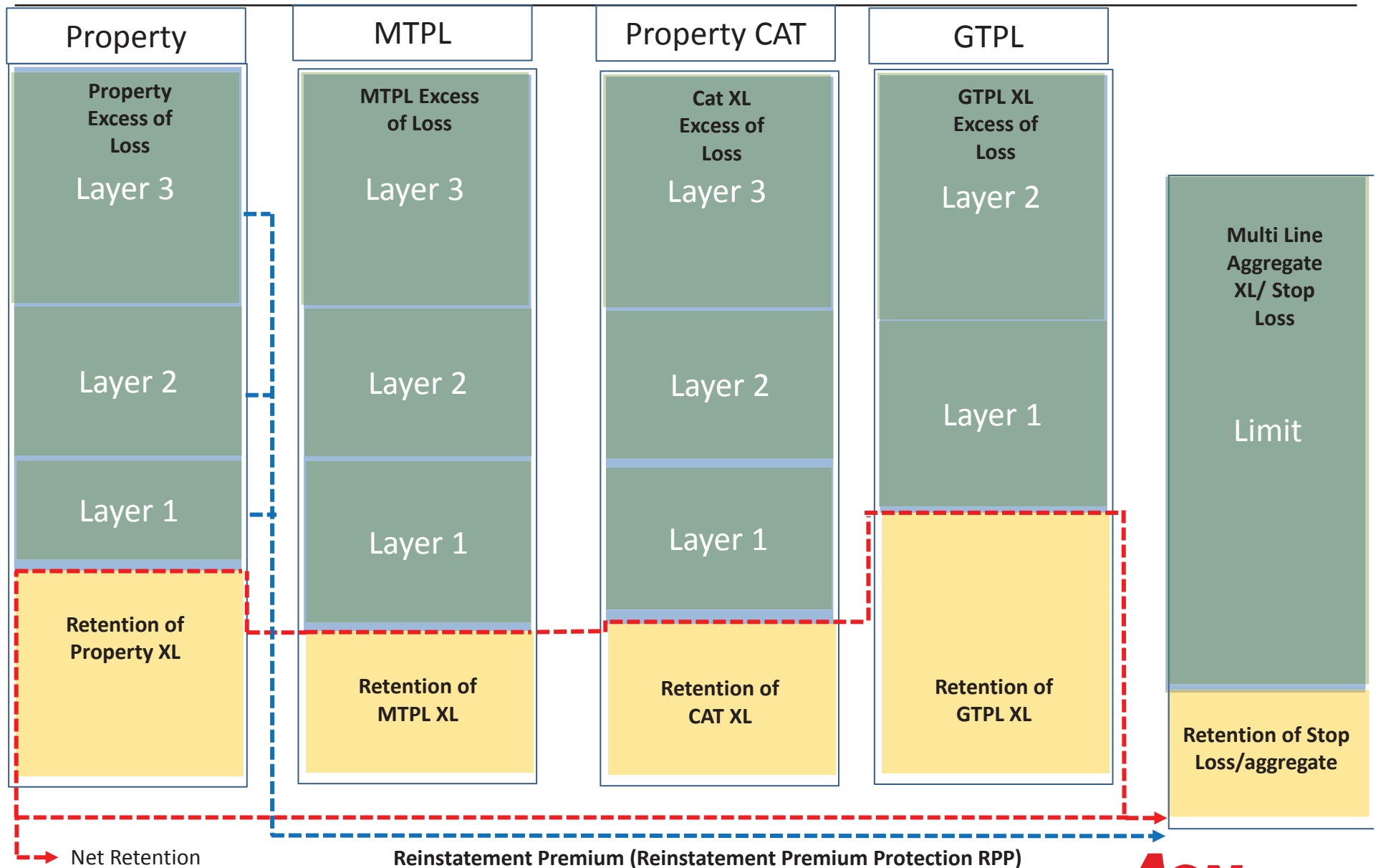


# Reinsurance Structuring Property





# Reinsurance Structuring “Gross XL Structure”





# Reinsurance Structure Optimization

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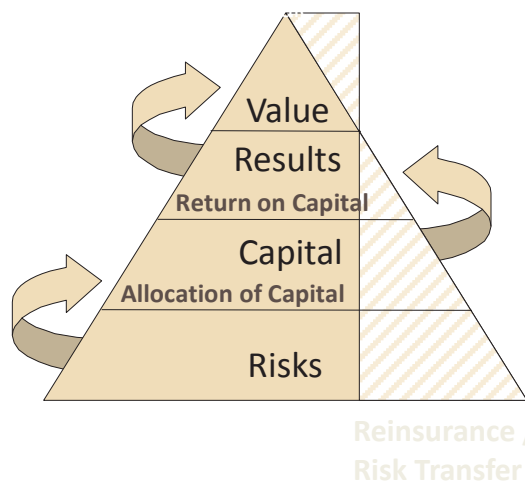
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# Measuring the efficiency of reinsurance

## Some key considerations for assessing the efficiency of reinsurance programmes

1. **Cost of reinsurance (premiums – Recoveries and commission paid on average)** : it is on average the amount paid on average to get the reinsurance cover
2. **Volatility transferred** : it is the reduction of the volatility of the result of the insurer thanks to the reinsurance cover
3. **Value created**: Value is created when the return on capital is higher than the cost of capital
4. **Ceded Return on Equity** : it is the profitability that the insurer would have on the business ceded to the reinsurer

**Risk transfer at a cost below  
the internal CoC creates value**



**4. How much value created?**

**3. Cost of ceded RoE?**

**2. How much capital released?**

**1. How much volatility transferred?**

**Value created = CoC \* (Gross Required Capital – Net Required Capital) – Cost of Reinsurance**

Cost of Capital

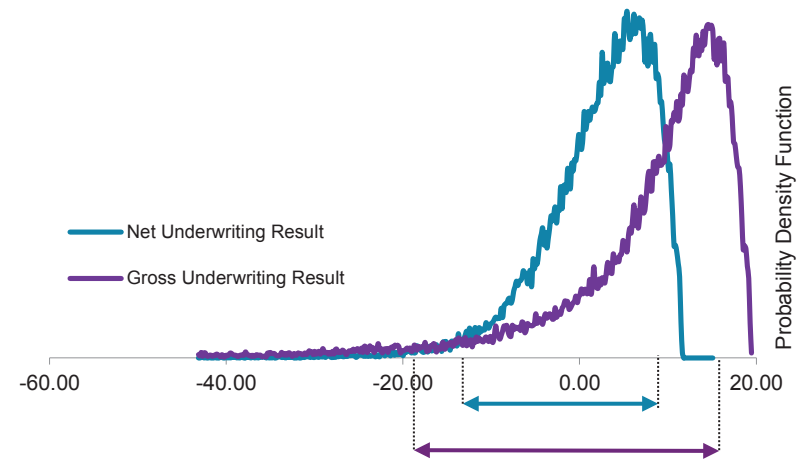
Capital Savings

# Key Reinsurance Metrics to Look at...

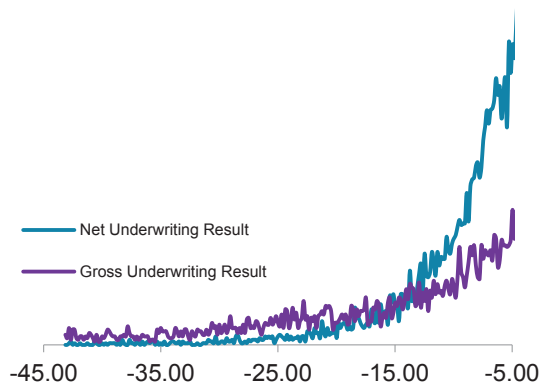
## 1. Reinsurance result - mean

$$\text{Expected Recovery from Reinsurers} - \text{Reinsurance Premium} = \text{Technical RI result (Insurer's cost)}$$

## 2. Volatility of Net UW Result



## 3. Tail Risk



## 4. Ceded ROE (Return On Equity)

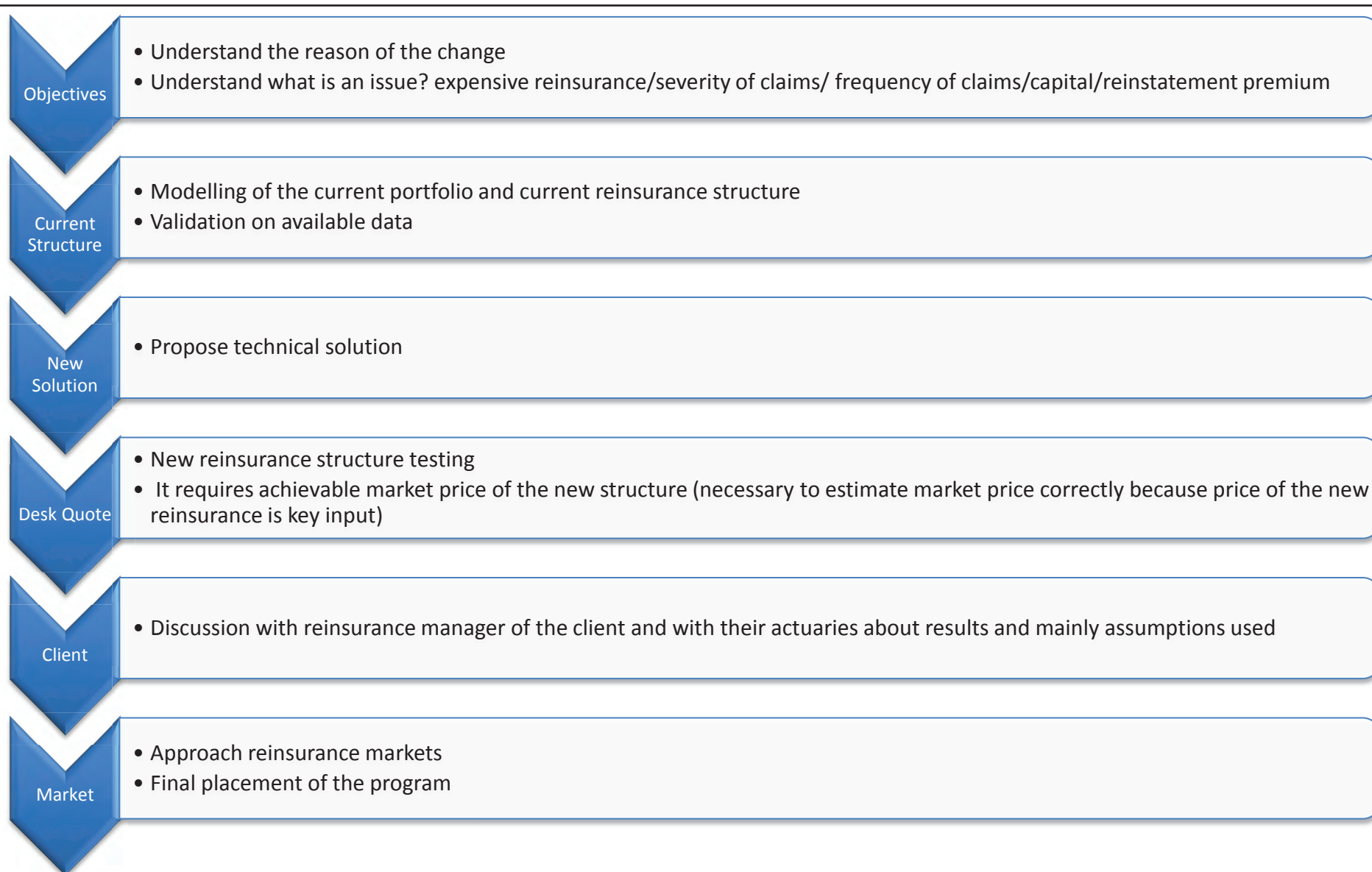
$$\text{Ceded ROE} = \frac{\text{Mean cost of reinsurance}}{\text{Decrease of capital due to reinsurance}}$$

# Introducing the concept of Ceded RoE

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- Ceded ROE = 
$$\frac{\text{Mean cost of reinsurance}}{(\text{Decrease of capital due to reinsurance})}$$
  - Where:
    - Mean cost of reinsurance = Reinsurance premium + Mean reinstatement premiums – mean of commissions – mean recoveries
    - Capital in this case is defined as how much capital is needed so that the company has 99,5% chance to pay for the claims (other definitions are possible)
- The ceded RoE represents the profitability that the insurer would have on the business that is ceded to the reinsurer. The lower this rate is the better it is to reinsure.
- Ideal measurement for comparing alternative Reinsurance strategies

# Key Steps in Reinsurance Optimization



# Questions?

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Ďakujem pekne za pozornosť!

Pekného Mikuláša prajem!





# Contact

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# Sources

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## **Slide : Before...**

NOTES ON THE ORIGIN AND DEVELOPMENT REINSURANCE BY EDWIN W. KOPF , individual websites of reinsurance companies

## **Slide: Reinsurance Market Concentration**

**Global Premium Volumes: insurance, reinsurance & retrocession (USD bn):** Reinsurance and Financial Stability, International Association of Insurance Supervisors, p.9  
Institute of Insurance Science, An Introduction to Reinsurance

## **Slide: Reinsurance Market is Global**

**Gilbert note:** REINSURANCE and International Financial Markets, Group of Thirty Wahsington DC 2006, p. 11

**US Gulf 2005 Huricanes Losses Payments:** Katrina, Wilma and Rita:Reinsurance and Financial Stability, International Association of Insurance Supervisors, p/